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NAVAL POSTGRADUATE SCHOOL Monterey, California



THESIS

DISTRIBUTIONAL ANALYSIS
OF INVENTORY
DEMAND OVER LEADTIME

bу

Mark Lee Yount

June 1982

Thesis Advisor:

Charles F. Taylor, Jr.

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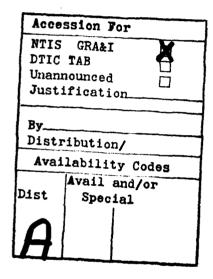
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Distributional Analysis
of Inventory
Demand Over Leadtime

by

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A BSTRACT

The distribution of inventory demand over procurement leadtime is modeled using mixed probability distributions that explicitly account for the high incidence of zero demands observed in Inventory Control Point Demand History Files. Analysis was limited to the right-hand tail area of the distribution on the assumption that that area is of critical importance in determining the effectiveness of an inventory system. Probabilistic models studied were: 1) Bernoulli-exponential, 2) B rnoulli-lognormal, and 3) Bernoulli-logistic. These compound distributions were compared to several standard distributions including the Poisson, negative binomial and normal distributions using a resampling procedure appropriate in cases such as this where a paucity of data exists. Fits obtained from the 75th to 95th percentiles indicated the mixed distributions may be superior as a class to the standard distributions for highdemand items.

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I. INTRODUCTION

Inventory system performance in a situation with random demand depends upon reorder point computations. Reorder point computations depend upon the probabilistic model chosen to represent the inventory system in that the reorder point is composed of two parts: 1) The expected demand during a procurement leadtime and 2) The safety level3 determined from the probabilistic model of demand over leadtime. Probabilistic models are generally only utilized to represent demand over procurement leadtime since that is the only time period when stockouts potentially occur. The chosen distribution is then a conditional distribution given procurement lead-The Navy has historically used three distributions of demand for models utilized at the Inventory Control Point (ICP) echelon of the Navy Supply System. The current probabilistic models and the average annual demand that is used to determine which model to utilize are displayed in Table 1.5

¹ See Appendix A for definition of "System Performance".

² See Appendix A for definition of "Reorder Point".

³ See Appendix A for definition of "Safety Level".

^{*}See Appendix A for definition of "Stockouts".

⁵The Aviation Supply Office (ASO) has recently changed to the use of the normal distribution as the model of choice for

Table 1: Current Inventory Control Point
Probabilistic Demand Over Leadtime Models

<u>Distribution</u>	Average Annual <u>Demand Range</u>
Poisson	0 - 1 Low
Negative Binomial	1 - 20 Medium
Normal	> 20 High

examined, one striking characteristic that is present in nearly all records is the high incidence of zero observations. This is not surprising when one considers the echeloning of the supply system and the fact that users only place a demand on the wholesale system as their reorder points are reached. Since most activities stock at least one quarter's expected demand for an item, reorders are expected at most four times a year. By the natural phase differences of each activity's reorder actions, the ICP may experience zero demands during a given quarter for even high-demand items, and will surely often experience quarters of zero demands for medium- and low-demand items. A previous study of Pacific Fleet Combat Stores Ships' demand data [Ref. 1] found that the frequency of zero observations in those demand

all demand categories. Ships Parts Control Center (SPCC) still uses all the distributions in Table 1.

records appeared to have a low correlation with the overall demand level (i.e. high, medium or low).

A desirable model for an inventory system should compute reorder levels that accurately correspond to a specified stockout risk based on the level of actual or anticipated demand for each item. If such a model were available, the inventory system could avoid the added expense of either having too much or too little stock. One problem with the distributions in Table 1 is that none can account for the probability mass at zero; therefore, none can accurately compute reorder levels.

This study explores the use of compound probability models and their potential to more accurately achieve the goals presented above by explicitly accounting for the probability mass at zero. The results obtained should be considered as a first step in the exploration of a class of models which have heretofore received little attention in the context of modeling inventory demand.

^{*}See Section II.B.1 for a more detailed discussion of this study.

II. BACK GROUND

A. CURRENT MODEL SELECTION TECHNIQUES

In the past, the usual approach of choosing the probabilistic model for lead time demand was based on matching the empirical cumulative distribution function determined from the actual demand to various theoretical cumulative distribution functions. The shapes of the two curves are compared using the Kolmogorov-Smirnov Statistical Goodness of Fit test. The Chi-Squared test has historically not been used because it is not very powerful when the number of observations is small (supply demand data is retained for at most twelve quarters and usually only eight quarters at the ICP level). The Kolmogorov-Smirnov test provides only a relative measure of goodness of fit, but it is usable with very small sample sizes. The goal then is to select the model with the best agreement between the empirical and theoretical cumulative distribution function curves.

The Navy Fleet Material Support Office (FMSO) has utilized the above Kolmogorov-Smirnov test to evaluate several theoretical distributions. Most recently [Ref. 2] FMSO

⁷A good description of the Kolmogorov-Smirnov one and two-sample tests may be found in Siegel, S., Non Parametric Statistics, p.47-52 and 127-136, McGraw Hill, 1956.

evaluated seven distributions at the 90% confidence level using demand data from NAS Brunswick. The use of demand data from a stock point vice an ICP assumes the underlying demand behavior at the stock point and ICP are similar. Though this was never validated directly, the NAS Brunswick demand data were deemed to have "unique qualities better suited for demand analysis" as follows:

- Twelve quarters of demand and demand frequency data were available per item, 50% more than available in ICP files,
- 2. New item identifiers that permit the selection of only steady state demand items were available,
- 3. Reliability of the data was established from prior FMSO studies.

The PMSO analysis showed that Navy demand patterns are very poorly modeled by any of the seven distributions studied. No new models were proposed and no attributes of the demand patterns were indicated as the most significant factor in the failure of the standard distributions to model Navy demand patterns.

There are several problems with the way the Kolmogorov-Smirnev test was used in the PMSO study:

^{*}Distributions tested were: Normal, Negative-Binomial, Poisson, Logistic, LaPlace, Gamma and Uniform.

- 1. The procedure is not strictly applicable in the case of discrete distributions such as the Poisson and negative binomial.
- 2. The test assumes that the parameters of the distribution being tested are completely specified in advance, i.e. not estimated from the data. (Lilliefors [Ref. 3] developed alternate tables for use in testing the exponential distribution when parameters are estimated from the data. This procedure was used in Reference 1.)
- 3. The Kolmogorov-Smirnov test evaluates goodness-of-fit over the entire range of the distribution. For inventory problems, the region of greatest interest is the right-hand tail of the distribution.

B. PREVIOUS RESEARCH

Research into distributions which have properties that more closely model actual demand patterns has been very limited and, when conducted, often did not explore anything but the usual standard distributions. Two projects though stand out because of their innovative use of non-standard distributions and the good fit achieved.

1. Bernoulli-exponential Distribution

In Reference 1, Pacific Fleet Combat Stores Ship demand was modeled using the mixed Bernoulli-exponential

distribution. This distribution was chosen because it was observed that nearly all line items had an unusually high occurence of demands of zero. Analysis of the data indicated that with high probability, the number of non-zero observations for a given item was unrelated to the average value of those non-zero observations. The conclusion was that the demand process could be thought of as two independent subprocesses with one process determining whether a demand would occur or not and the other determining the quantity of the demand, given the demand did occur. The former process was modeled as a Bernoulli process with parameter p, p being the probability that a demand did occur. The latter process was modeled as a continuous exponential process based on exploratory data analysis. The resulting probability distribution function for the number of units demanded in a leadtime for the Bernoulli-exponential distribution is given by:

$$h(x) = \begin{cases} 1 - p, & x = 0 \\ p \lambda e x p(-\lambda x), & x > 0, \end{cases}$$
 (1)

where:

 $1/\lambda$ = the expected value of demand, given that the demand is greater than zero.

p = probability that demand does occur.

The complementary cumulative distribution function is given by:

$$H(x) = p \exp(-\lambda x), \quad x \ge 0, \tag{2}$$

where H(x) is the probability that demand will not exceed x; this is equivalent to the complementary cumulative distribution function used by Hadley and Whitin [Ref. 4].

The hypothesis that the demand of Combat Stores Ships could be modeled according to the above probability distribution was tested using the Kolmogorov-Smirnov test described earlier plus tests on the theoretical risk and the observed risk for values of risk in the upper right hand tail area of the distribution. The results of these tests on five independent samples from the demand data available provided strong evidence that the Bernoulli-exponential distribution describes the demand for any given stock item very well.

2. Logarithmic-Poisson-Gamma Distribution

A model for the distribution of demand during procurement leadtime [Ref. 5] was derived under the following assumptions:

- a. Requisitions occur according to a stationary Poisson Process.
- b. Requisition sizes follow a logarithmic distribution,

c. Leadtime is a random variable with the gamma distribution.

The resulting probability function for the number of units demanded in a leadtime is:

$$h(x) = \left(\frac{\beta}{\lambda + \beta}\right)^{\alpha} - \frac{\theta}{x!} \sum_{k=1}^{x} \left(\frac{z}{\lambda + \beta}\right)^{k} s_{x,k} \sum_{j=1}^{k} s_{k,j}$$
(3)

for x = 1, 2, 3, ...

an d

$$h(0) = \left(\frac{\beta}{\lambda + \beta}\right)^{\alpha}$$

where:

 α, β = parameters of the Gamma distribution defining leadtime.

 Θ = parameter of the logarithmic distribution solved for by interval bisection from $E(X) = -\Theta / (1 - \Theta) \ln (1 - \Theta),$

 λ = requisition arrival rate,

 $c = -\lambda / \ln (1 - \Theta)$

 $S_{x,k}$ = Stirling numbers of the first kind computed from the recursion

$$S_{x,k} = S_{x-1,k-1} + (x - 1) S_{x-1,k}$$

for k = 1, 2, ..., x and x = 1, 2, ...
with $S_{x,0} = 0$ for all x

This distribution is called the Logarithmic-Poisson-Gamma (LPG). It is defined from four parameters α , β , θ , and λ (θ and λ determine c).

For more efficient computations, a recursion equation for integer α was developed.

$$h(x) = \sum_{k=1}^{x} T_{x,k}$$
 (4)

where:

$$T_{x,k} = \frac{\theta}{x} [C_2(\alpha + k - 1)T_{x-1,k-1} + (x - 1)T_{x-1,k}]$$
 $C_2 = c / (\lambda + \beta)$

and θ , c, α , β and λ defined as in (3).

Computing reorder points from fractiles of the LPG distribution, even using the simplified version of (4), is generally too time consuming for many real applications. As a result, an approximation was developed and tested that used a scaled version of the Poisson distribution to approximate the negative binomial distribution. The resulting approximation is:

$$p\{Z(t) = kx\} \simeq \frac{(\alpha + x - 1)!}{x! (\alpha - 1)!} \left(\frac{\beta}{\mu + \beta}\right)^{\alpha} \left(\frac{\mu}{\mu + \beta}\right)^{x}$$
for $x = 0, 1, 2, ...$

where:

Z(t) = number of units demanded in time t

 $\mu = c\theta$

 α , β , c and θ defined as in (3).

The authors conducted subjective tests of goodness of fit to their LPG model and its derivatives using Air Force consumable items and concluded, using as an example one item, that there was a "very close agreement between the observed and the predicted cumulative distribution functions for this item."

III. PROPOSED MODELS

A. COMPOUND BERNOULLI MODELS IN GENERAL

The results of the previous research indicate that a potential exists for improving inventory performance by the use of slightly more complex models. The focus of this study is on the compound Bernoulli models, leaving further analysis of the LPG model and its derivatives to others. The use of compound Bernoulli models has several advantages over standard simple distributions:

- 1. The model, by necessity, has an added parameter whose sole function is to estimate the probability of a non-zero demand.
- 2. For simple models defined only over the positive real numbers, the addition of the Bernoulli parameter simply results in the scaling of the cumulative distribution, thus adding little additional complexity to the model.
- 3. By explicitly accounting for zero demands, compound models account for more of the observed variance than do simple models.

Compound models are not without disadvantages:

 Each parameter added to the model must be estimated for each individual stock item. For a large inventory system such as the Navy's, this equates to considerable additional computational requirements.

2. Additional parameters must be stored for future retrieval or else computed from stored data when required, thus either extending computational time or else requiring additional online storage space.

The Bernoulli compound models all have similarly shaped cumulative distribution functions. Figure 1 is a sample distribution function for the compound Bernoulli-lognormal distribution with a Bernoulli factor of p equal to 0.6, a mean of 1.0 and a standard deviation of 0.5. Note that the distribution has a mass of zero for negative observations, a mass of 1-p at zero and the usual cumulative distribution function shape for positive observations but of mass p vice mass one.

B. MODEL DESCRIPTIONS

Three compound Bernoulli models were formulated for evaluation. Each model was derived from the base distribution after compounding with the Bernoulli process. An additional requirement was made that the inverse of the compound model must be computationally relatively simple.

1. Bernoulli-exponential Distribution

This distribution was derived in Reference 1 and the derivation will not be repeated here. Equations (1) and (2)

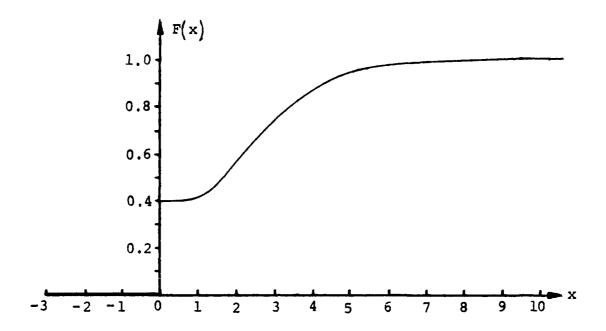


Figure 1: Compound Cumulative Distribution Function,

Bernoulli-lognormal Distribution

are the probability density and complementary cumulative distribution functions respectively. The Bernoulli-exponential inverse complementary cumulative distribution function is computed as:

$$x = \begin{cases} 0 & \text{, } H(x) \ge p \\ \mu[\ln(p) - \ln(H(x))], H(x) (6)$$

The parameters of this distribution are estimated from the sample data as follows:

- p = number of non-zero demand observations in sample divided by sample size,
- $\hat{\mu} = \bar{x}$ / \hat{p} , where \bar{x} is the entire sample mean, or
 - $\hat{\mu} = \bar{x}$, where \bar{x} is the sample mean of only the non-zero demand observations.

2. Bernoulli-lognormal Distribution

The lognormal distribution was chosen as a candidate for testing because of several desirable properties:

- a. It is defined for all real numbers greater than zero,
- b. Its inverse is readily computed using inverse normal approximations that are well documented for accuracy,
- c. Alone, the lognormal distribution does not allow the case of zero demand, but when combined with the Bernoulli distribution, the compound Bernoulli-lognormal distribution defines all the expected demand values greater than or equal to zero.

Utilizing the Bernoulli parameter p as a scaling factor for the lognormal density function, the compound Bernoulli-lognormal density function may be expressed as:

$$h(x) = \begin{cases} 1 - p, & x = 0 \\ p\phi(\frac{\ln(x) - \mu}{\sigma}, & x > 0 \end{cases}$$
 (7)

where:

- p = probability of a non-zero demand,
- μ = mean of the natural log of all demands greater than zero,
- σ = Standard deviation of the natural log of all demands greater than zero,
- ϕ = Standard normal density function. Integrating (7) results in the complementary cumulative distribution function given by:

$$p \qquad , x = 0$$

$$H(x) = p \left[1 - \phi \left(\frac{\ln(x) - \mu}{\sigma}\right)\right], x > 0$$
(8)

where:

 Φ = Standard normal cumulative distribution function. The Bernoulli-lognormal inverse cumulative distribution function is easily derived from (8) as:

$$\mathbf{x} = \begin{cases} 0 & \text{, } H(\mathbf{x}) \ge p \\ \exp[\mu + \sigma \phi^{-1} (1 - H(\mathbf{x})/p)], H(\mathbf{x}) (9)$$

The parameters are estimated from the sample data in the usual manner:

p = number of non-zero demand observations in sample divided by sample size,

- $\hat{\mu} = \bar{x}$, where \bar{x} is the sample mean of the natural log of all non-zero demand observations,
- \$\hat{\text{\$\te

3. Bernoulli-lcqistic Distribution

The logistic distribution is a pseudo-normal distribution that is similar in shape to the normal, but is easier to handle mathematically. Its density function is defined as [Ref. 6]:

$$f(x) = \frac{\pi}{4\sqrt{3}\sigma} \operatorname{sech}^{2}\left(\frac{\pi(x-\mu)}{2\sqrt{3}\sigma}\right), -\infty < x < \infty,$$
 (10)

while its cumulative distribution function is defined as:

$$F(x) = \frac{1}{2} \left[1 + \tanh \left(\frac{\pi (x - \mu)}{2\sqrt{3} \sigma} \right) \right], -\infty < x < \infty,$$
 (11)

where:

 $\mu = mean of the entire sample,$

 σ = standard deviation of the entire sample.

With the logistic distribution, it is no longer a simple matter of scaling the distribution by the Bernoulli p parameter, since this distribution is defined over the entire real line and not just on the positive half. Consequently, the distribution requires a new constant of integration to replace the 1/2 used in (11). Integrating (10) from 0 to ∞ provides the new constant as:

$$\int_{0}^{\infty} \operatorname{sech}^{2}\left(\frac{\pi(x-\mu)}{2\sqrt{3}\sigma}\right) dx = 1 + \tanh\left(\frac{\pi\mu}{2\sqrt{3}\sigma}\right)$$
 (12)

which, when compounded with the Bernoulli distribution, gives the Bernoulli-logistic distribution density function as:

where:

 μ = mean of all non-zero demand observations,

σ = standard deviation of all non-zero demand observations.

After integrating (13), the complementary cumulative distribution function may be written as:

$$H(x) = p \left\{ 1 - \frac{1}{2\sqrt{3}\sigma} \right\} \left\{ \tanh\left(\frac{\pi\mu}{2\sqrt{3}\sigma}\right) + \tanh\left(\frac{\pi(x-\mu)}{2\sqrt{3}\sigma}\right) \right\}$$
(14)

for $x \ge 0$

The inverse cumulative distribution is:

$$\mathbf{x} = \begin{cases} 0 & \text{, } H(\mathbf{x}) \ge p & (15) \\ \mu + \frac{\sqrt{3}\sigma}{\pi} \left\{ \frac{2p}{H(\mathbf{x}) \left[1 + \tanh\left(\frac{\pi\mu}{2\sqrt{3}\sigma}\right) \right]} - 1 \right\}, H(\mathbf{x}) \le p \end{cases}$$

The parameters are estimated from the sample data in the usual manner:

- \hat{p} = number of non-zero demand observations in sample divided by sample size,
- $\hat{\mu} = \bar{x}$, where \bar{x} is the sample mean of all non-zero demand observations,
- $\hat{\sigma}$ = s, where s is the sample standard deviation of all non-zero demand observations.

IV. EVALUATION PROCEDURE

A. THE DATA

In order to test the validity of the proposed models, samples of actual demand were obtained from the Operations Analysis Department at PMSO. The data, accumulated from the demand history files of the Aviation Supply Office, was originally used as input data for the 5A (Aviation Afloat and Ashore Allowance Analyzer) [Ref. 7]. The data consists of 1587 consumable 1R cog items and 2892 non-program-related9 repairable 2R cog items. The information for each item is contained in one master record and several subrecords. The master record contains identifying information on each item such as the national stock number, replacement price, etc. Each subrecord contains up to forty-six demand records, each including the demand quantity and the day of the demand. A complete record layout is contained in Appendix E. To ease processing, the Julian Dates of the original demands were replaced by FMSO with a sequential date ranging from 1 to 1500 representing approximately four years of available history.

^{*}See Appendix A for definition of "program related" items.

For this application, additional screening was conducted to group the demands into thirty-day buckets, thus providing a demand time series of forty-eight observations. Further editing was required prior to analysis to remove the negative demands noted for many of the items. It was assumed that the negative observations were the result of cancellations of previous demands which were never filled. Therefore, whenever a negative demand was encountered, the demand series was searched backwards for the first positive demand equal to or larger than the negative demand. If such a demand was found, the positive demand quantity was reduced by the absolute value of the negative quantity and the negative quantity was set equal to zero. If no offsetting positive demand was found, the negative demand quantity was still set equal to zero. The resulting edited demand time series was used as the base for all further analysis. Iwo additional demand series were created from the edited series:

- 1. A demand series of only the non-zero demands,
- 2. A demand series of the log of the non-zero demands.

 The sample mean and sample standard deviation for each of the three demand series were computed on and the group, representing one line item, was accepted for futher processing if:

¹⁰Stationarity was assumed for the demand time series under study. If a trend were in fact present, the resampling technique effectively would eliminate it by shuffling the observed demands into random order.

- 1. There were at least two non-zero demands, and
- 2. The standard deviation of all three series was non-zero.

Once accepted, the sample mean and/or sample standard deviation of the appropriate series was used to estimate the value of x, such that for a given probability, demand will not exceed that value of x. The values of x were computed for each model tested at several probabilities from the inverse cumulative probability functions. Table 2 displays the sample mean and/or sample standard deviation required for each model investigated.

B. THE RESAMPLING PROCEDURE

The resampling procedure used was chosen over the more traditional methods discussed in Chapter II because it provides a method of comparing a theoretical distribution to the sample data at specified probabilities and is applicable in cases such as this where there is a paucity of data available for analysis. This procedure is similar to the "bootstrap" procedure used by Efron [Ref. 8]. The idea behind this procedure is to randomly sample with replacement the series of available data to create additional pseudo-samples that possess the same statistical properties as the original sample. The desired statistical property can then be estimated from

Table 2: Required Data for Inverse Computations

MODEL	MEAN	STANDARD <u>DEVIATION</u>
Exponential	A	N/R
Normal	A	A
Poisson	A	N/R
Negative Binomial	A	A
Lognormal	С	С
Logistic	A	A
La Place	A	A
Bernoulli-exponential	В	N/R
Bernoulli-lognormal	С	С
Bernoulli-logistic	В	В
	Exponential Normal Poisson Negative Binomial Lognormal Logistic La Place Bernoulli-exponential Bernoulli-lognormal	Exponential A Normal A Poisson A Negative Binomial A Lognormal C Logistic A La Place A Bernoulli-exponential B Bernoulli-lognormal C

Where:

- A is from edited demand series
- B is from non-zero demand series
- C is from log of non-zero demand series
- N/R indicates parameter Not Required for this model

each pseudo sample. With a sufficient number of repetitions, the distribution of the estimated property is known to be normal from the central limit theorem with mean equal to the population mean and standard deviation equal to the population standard deviation divided by the number of repetitions.

Thus by the use of the resampling procedure, it is possible to study theoretical distributions at points in their

right hand tail area, which is the region of most interest in computing safety levels in inventory models. The resampling procedure, as applied in this study, is a relatively straightforward application of the following technique:

- 1. The edited series for each sample of n demand observations is treated as the population from which the random samples are drawn.
- 2. A random sample of size n is drawn from this population, creating a pseudo sample. The pseudo sample is not a permutation of the original population since the sample values are selected with replacement from the original population. This is easily accomplished in a computer by generating n uniform random integers in the range from 1 to n, and using these numbers as subscripts to select the sample from the original population.
- 3. The pseudo sample percentile is computed for each repetition from (16) and is compared to the theoretical percentile.
 - $\hat{\rho}$ = (number of demand observations \leq x) / n (16) The various values of x are computed from the inverse cumulative probability functions for each model evaluated.

Under the null hypothesis that the sample demands come from a particular probability distribution, the expected value of $\hat{\rho}$ should equal ρ , the theoretical percentile:

$$E[\hat{\rho}] = \rho \text{ under } H_O \tag{17}$$

and the distribution of ρ should be Normal($\rho,\sigma^2/n$). The percentile ρ is estimated as above and σ^2 is estimated from standard binomial results as:

$$Var[\hat{\rho}] = \hat{\rho}(1 - \hat{\rho}) / n. \tag{18}$$

C. MEASURES OF EFFECTIVENESS

When the above precedure is executed at several theoretical percentiles, the fit of the sample data may be compared at several locations in the theoretical distribution and the overall fit evaluated. Several common measures of effectiveness are available to provide a criteria on which to judge the success or failure of a model. Some of those available are:

- 1. Maximum absolute deviation,
- 2. Mean squared error,
- 3. Algebraic sum of errors.

Method three was eliminated since errors may offset one another resulting in a seemingly good fit, but in reality a

very poor fit. Method one is potentially a good way to evaluate error, but is generally not as sensitive as method two. Therefore, the mean squared error of the pseudo sample percentile estimates was chosen as the measure of effectiveness of 'choice and was accumulated as:

$$MSE = \frac{1}{n} \sum_{i=1}^{n} (\hat{\rho}_{i} - \rho_{i})^{2}.$$
 (19)

D. COMPUTER VALIDATION

The computer programs for this analysis were written in FORTRAN IV for execution on the IBM 3033 attached processor (System 370) computer installed at the Naval Postgraduate School. The programs are batch oriented since the volume of data available prevented storage directly on the user's private disk space. The data tapes received from PMSO were loaded onto the system mass storage device and when required, all or portions of the data were transferred to the Virtual Machine (VM) facility for processing. Two programs were written, the first to copy the data to make it accessible to the VM system and the second to conduct the actual analysis. A complete listing of the FORTRAN source code is available in Appendix F. Each program or subprogram contains a documentation block at the top that provides a complete description of

the program's purpose, a definition of variables used and a list of user-written subroutines and functions required.

The random number generator used is a part of the LLRANDON II series [Ref. 9] developed at the Naval Postgraduate School. The programs and subprograms were thoroughly tested both independently and as a unit using known data. The results were verified by hand held calculator and in all cases agreed with the program output.

V. RESULTS

The results of the distributional analysis conducted on the ten distribution models listed in Table 2 are tabulated in Appendix B for 1R consumable items. Appendix B is divided into the three demand classes listed in Table 1, and then each class is divided by distribution and percentile within each distribution. The results for the 2R repairable items are presented in a similar format in Appendix C.

The consistency of the resampling method with varying data was evaluated by testing independent sections of the consumable and repairable data sets and comparing the results. In both cases, independent subsamples were created by sampling every third item but changing the initial item sampled from the first to the third item. The analysis, not presented here, showed that the resampling method produced consistent results over all of the subsamples tested. The total mean square error of the distributions in each subsample varied by no more than 20% from the total mean square error values obtained from the entire sample population as listed in Appendix B and Appendix C. The relative standing

¹¹Total mean square error is the sum of the mean square errors computed at the 75th, 80th, 85th, 90th and 95th percentiles.

of each distribution was not altered in any of the subsamples.

The effect of the number of pseudo sample repetitions was also studied. The results proved similar while varying the number of repetitions from twenty to fifty. The standard deviation of the percentile estimates decreased as the number of repetitions increased. The total mean square error for each trial varied randomly but remained within 10% of the overall values for each distribution with more repetitions producing consistently smaller variations. For the data analysis production runs, forty was chosen as the number of resampling repetitions as a trade off between computer run time and minimizing variance.

A. LOW-DEMAND ITEMS

A summary of the total mean squared error figures for the models providing the best fit or the smallest total mean squared error is provided in Table 3 for the low-demand items. The best models for the low demand items all had very small total mean squared errors. This can be attributed to the very low probability of a demand ever being greater than one and to the integer sampling plan for accumulating the Bernoulli trials. For the integer results of the Poisson and negative binomial distributions, the estimated percentile

TABLE 3: LOW-DEMAND ITEMS,

Total Mean Squared Error (10-4)

	<u>Poi sson</u>	Negati v e <u>binomial</u>	Compound
Consumable 1R	5.64	7.86	10.77
Repairable 2R	5.86	7.57	12.91

will closely match the theoretical percentile unless the number of Bernoulli successes is less than the expected number of successes for a given theoretical percentile. This produces a conservative result that will tend to overstate the quantity of stock required by one unit to provide a stated level of protection, but in the case of the small quantities involved, is not an undesirable praperty. The compound distributions, as a group, gave the same total mean squared error for much the same reasons. The probability of a nonzero demand is very small for the low-demand items, generally less than 0.05, thus these models tend to predict a quantity of zero for all percentiles. The resampling procedure and the sampling plan again provide a conservative result.

B. MEDIUM-DEMAND ITEMS

A summary of the total mean squared error figures for the models providing the best fit or the smallest total mean

squared error is provided in Table 4 for the medium-demand items. Here again the predicted demand for the various percentiles is small. The resampling technique still gives the

TABLE 4: MEDIUM-DEMAND ITEMS,

Total Mean Squared Error (10-4)

	Negative <u>binomial</u>	<u>Poisson</u>	Bernoulli- lognormal
Consumable 1R	28.55	48.28	80.60
Repairable 2R	29.14	44.84	112.44

edge to the integer distributions. The compound distributions have begun to show some differences among themselves, but as a group are clearly better than any of the continuous simple distributions. The magnitude of the total mean squared error is significantly larger than for the low-demand class primarily due to the larger allowable total demand range defining the medium-demand class.

C. HIGH-DEMAND ITEMS

The summary total mean squared error data for the high-demand items are listed in Table 5. With the unlimited range of mean demands in this class, the higher total mean squared errors are expected. The compound models have come into

TABLE 5: HIGH-DEMAND ITEMS,

Total Mean Squared Error (10-4)

	Bernoulli- lognormal	Bernoulli- exponential	<u>Exponential</u>
Consumable 1R	168.25	188.90	298.21
Repairable 2R	183.77	221.80	289.01

their own in this class with the Bernoulli-lognormal yielding a total mean squared error less than one half that of the normal distribution. The second best distribution, the Bernoulli-exponential, gives a total mean squared error only slightly higher than the Bernoulli-lognormal.

VI. CONCLUSIONS AND RECOMMENDATIONS

A. SUMMARY

This distributional analysis, conducted using a completely different experimental procedure than prior analyses, provides satisfyingly similar results for the low and medium demand categories in showing that the Poisson distribution gives the best fit for the low-demand category of items and that the negative binomial distribution gives the best fit for the medium-demand category of items. The class of compound distributions, as a whole, gave good fits in the low-and medium-demand categories, though the total mean squared error was two to four times as large as that of the Poisson or negative binomial distribution.

The analysis indicated that there are several distributions which provide better results than the normal distribution for high-demand items. The Bernoulli-lognormal distribution consistently provided total mean squared errors approximately one half that of the normal distribution, indicating a superior fit in the right-hand tail area of the distribution. Other distributions giving good fits were the Bernoulli-exponential and the standard exponential, both yielding total mean squared errors less than that of the normal distribution.

B. RECOMMENDATIONS

The results of this study indicate the Navy should continue to use the Poisson and negative binomial distributions as the models for the low- and medium-demand classes respectively. Specifically, the Aviation Supply Office should reevaluate its position on the use of the normal distribution for all demand classes and revert to the Poisson and negative binomial distributions for low- and medium-demand classes as before. The normal distribution tends to inflate the stock required for low- and medium-demand items for a specified level of protection resulting in increased safety levels and excessive dollar investment.

The Navy should consider replacing the normal distribution model used for high-demand items with the compound Bernoulli-lognormal distribution. If the Bernoulli-lognormal distribution is considered computationally too difficult for a large inventory system, the Bernoulli-exponential could be used in its place with little loss of effectiveness.

C. ADDITIONAL RESEARCH

Follow on research in the following areas may improve and expand upon the results presented above:

1. Optimize the divisions of demand categories (i.e. low, medium, high) with the possible use of the probability

- of a non-zero demand as an element in the determination,
- 2. Implement the Bernoulli-lognormal model in FMSO's 5A simulator to establish the effect of the change on the entire supply system,
- 3. Investigate the implications of the assumption that the demand process is stationary,
- 4. Evaluate other compound distributions, such as the Bernoulli-log-logistic, which is particularly appealing analytically.

AP PENDIX A

GLOSS ARY OF TERMS

Program Related Item: An item of stock whose demand can be predicted from the value of a specific Navy program, i.e., flying hours, steaming hours, etc.

Reorder Point: The on hand stock quantity that when reached, triggers an order for replenishment of stock material. The reorder Point is the expected demand during procurement lead-time plus the safety level.

Risk: Probability of a stockout during leadtime.

Safety Level: The quantity of material which is required to be on hand to permit continued operation in the event of minor interuptions on normal replenishment or unpredictable fluctuations in demand. The safety level determined is structured so as to minimize time-weighted, essentiality-weighted requisitions short.

Stockout: A condition that exists when the on hand inventory is insufficient to fill the current demand requirements.

System Performance: A subjective measure maximized when the time-weighted, essentiality-weighted requisitions short is minimized. Time weighting is the consideration of the average number of days delay in the availability of material, essentiality-weighting is the consideration of the relative essentiality of each item. Requisitions short are requisitions for which material is not available.

APPENDIX B

CONSUMABLE ITEM TABULATED RESULTS

40 REPETITIONS FOR EACH OF 61 PSEUDO SAMPLES

LOW DEMAND RANGE: 0.0 < D < 1.0 PER YEAR

DISTRIBUTION: POISSON

THEORETICAL PERCENTILES (P)

ESTINATES: 0.75 0.80 0.85 0.90 0.95

MEAN 0.750000 0.812500 0.854006 0.913924 0.956069

STD DEV 0.008766 0.007902 0.007148 0.005678 0.004149

MSE 0.0 0.000156 0.000018 0.000290 0.000100

TOTAL MSE: 5.64E-04

DISTRIBUTION: NEGATIVE BINOMIAL

THEORETICAL PERCENTILES (P)

ESTIMATES: 0.75 0.80 0.85 0.90 0.95

MEAN 0.750000 0.812500 0.854006 0.913924 0.948994

STD DEV 0.008766 0.007902 0.007148 0.005678 0.004454

MSE 0.0 0.000156 0.000018 0.000290 0.000322

TOTAL MSE: 7.86E-04

LOW DEMAND RANGE: 0.0 < D < 1.0 PER YEAR

DISTRIBUTION: NORMAL

THEORETICAL PERCENTILES (P)

 ESTINATES:
 0.75
 0.80
 0.85
 0.90
 0.95

 MEAN
 0.953221
 0.953221
 0.953221
 0.953221
 0.953221
 0.953221
 0.953221

 STD DEV
 0.004275
 0.004275
 0.004275
 0.004275
 0.004275
 0.004275

 MSE
 0.042319
 0.024488
 0.011662
 0.003835
 0.001006

TOTAL MSE: 833.09E-04

DISTRIBUTION: <u>EXPONENTIAL</u>

THEORETICAL PERCENTILES (P)

ESTINATES: 0.75 0.80 0.85 0.90 0.95

MEAN 0.953221 0.953221 0.953221 0.953221 0.953221

STD DEV 0.004275 0.004275 0.004275 0.004275

MSE 0.042319 0.024488 0.011662 0.003835 0.001006

TOTAL MSE: 833.09E-04

DISTRIBUTION: LOGNORMAL

THEORETICAL PERCENTILES (P)

 ESTIMATES:
 0.75
 0.80
 0.85
 0.90
 0.95

 MEAN
 0.978404
 0.995246
 0.995246
 1.000000
 1.000000

 STD DEV
 0.002943
 0.001392
 0.001392
 0.0
 0.0

 MSE
 0.052629
 0.038292
 0.021267
 0.009998
 0.002500

TOTAL MSE: 1246.85E-04

LOW DEMAND RANGE: 0.0 < D < 1.0 PER YEAR

DISTRIBUTION: LAPLACE

THEORETICAL PERCENTILES (P)

 ESTIMATES:
 Q.75
 Q.80
 Q.85
 Q.90
 Q.95

 MEAN
 0.953221
 0.953221
 0.953221
 0.953221
 0.953221
 0.953221

 STD DEV
 0.004275
 0.004275
 0.004275
 0.004275
 0.004275
 0.003835
 0.001006

TOTAL MSE: 833.09E-04

DISTRIBUTION: LOGISTIC

THEORETICAL PERCENTILES (P)

 ESTINATES:
 0.75
 0.80
 0.85
 0.90
 0.95

 MEAN
 0.953221
 0.953221
 0.953221
 0.953221
 0.953221
 0.953221

 STD DEV
 0.004275
 0.004275
 0.004275
 0.004275
 0.004275
 0.004275

 MSE
 0.042319
 0.024488
 0.011662
 0.003835
 0.001006

TOTAL MSE: 833.09E-04

DISTRIBUTION: <u>BERNOULLI-EX PONENTIAL</u>

THEORETICAL PERCENTILES (P)

ESTIMATES: 0.75 0.80 0.85 0.90 0.95

MEAN 0.750000 0.812500 0.854006 0.913924 0.944939

STD DEV 0.008766 0.007902 0.007148 0.005678 0.004618

MSE 0.0 0.000156 0.000018 0.000290 0.000613

TOTAL MSE: 10.77E-04

LOW DEMAND RANGE: 0.0 < D < 1.0 PER YEAR

DISTRIBUTION: BERNOULLI-LOGNORMAL

THEORETICAL PERCENTILES (P)

ESTIMATES: 0.75 0.80 0.85 0.90 0.95

MEAN 0.750000 0.812500 0.854006 0.913924 0.944939

STD DEV 0.008766 0.007902 0.007148 0.005678 0.004618

MSE 0.0 0.000156 0.000018 0.000290 0.000613

TOTAL MSE: 10.77E-04

DISTRIBUTION: BERNOULLI-LOGISTIC

THEORETICAL PERCENTILES (P)

ESTIMATES: 0.75 0.80 0.85 0.90 0.95

MEAN 0.750000 0.812500 0.854006 0.913924 0.944939

STD DEV 0.008766 0.007902 0.007148 0.005678 0.004618

MSE 0.0 0.000156 0.000018 0.000290 0.000613

TOTAL MSE: 10.77E-04

MEDIUM DEMAND RANGE: 1.0 < D < 20.0 PER YEAR

DISTRIBUTION: PCISSON

THEORETICAL PERCENTILES (P)

ESTIMATES: Q.75 Q.80 Q.85 Q.90 Q.95

MEAN 0.748131 0.807719 0.843932 0.893923 0.925303

STD DEV 0.002501 0.002271 0.002091 0.001774 0.001515

MSE 0.000138 0.000398 0.000603 0.001423 0.002266

TOTAL MSE: 48.28E-04

DISTRIBUTION: NEGATIVE BINOMIAL

THEORETICAL PERCENTILES (P)

ESTINATES: 0.75 0.80 0.85 0.90 0.95

MEAN 0.746099 0.805430 0.843400 0.900210 0.943628

STD DEV 0.002508 0.002281 0.002094 0.001727 0.001329

MSE 0.000332 0.000522 0.000589 0.000807 0.000606

TOTAL MSE: 28.55E-04

DISTRIBUTION: NORMAL

THEORETICAL PERCENTILES (P)

ESTIMATES: 0.75 0.80 0.85 0.90 0.95

MEAN 0.888030 0.896699 0.907882 0.920152 0.935573

STD DEV 0.001817 0.001754 0.001666 0.001562 0.001415

MSE 0.024771 0.014168 0.007327 0.003509 0.002400

TOTAL MSE: 521.74E-04

MEDIUM DEMAND RANGE: 1.0 < D < 20.0 PER YEAR

DISTRIBUTION: EXPONENTIAL

THEORETICAL PERCENTILES (P)

ESTIMATES: 0.75 0.80 0.85 0.90 0.95

MEAN 0.852981 0.861003 0.871591 0.884311 0.898352

STD DEV 0.002040 0.001993 0.001928 0.001843 0.001741

MSE 0.020357 0.011779 0.006819 0.004953 0.006210

TOTAL MSE: 501.19E-04

DISTRIBUTION: LOGNORMAL

THEORETICAL PERCENTILES (P)

<u>ESTINATES:</u> 0.75 0.80 0.85 0.90 0.95

MEAN 0.953018 0.962552 0.970638 0.980623 0.990731

STD DEV 0.001219 0.001094 0.000973 0.000794 0.000552

MSE 0.043846 0.028367 0.015977 0.007411 0.002040

TOTAL MSE: 976.41E-04

DISTRIBUTION: LAPLACE

THEORETICAL PERCENTILES (P)

ESTIMATES: 0.75 0.80 0.85 0.90 0.95

MEAN 0.884254 0.893767 0.904733 0.918110 0.936078

STD DEV 0.001843 0.001775 0.001692 0.001580 0.001409

MSE 0.024079 0.013865 0.007191 0.003573 0.002363

TOTAL MSE: 510.72E-04

MEDIUM DEMAND RANGE: 1.0 < D < 20.0 PER YEAR

DISTRIBUTION: LOGISTIC

THEORETICAL PERCENTILES (P)

0.022871 0.013193 0.006955 0.003690 0.002447

 ESTIMATES:
 0.75
 0.80
 0.85
 0.90
 0.95

 MEAN
 0.875036
 0.886687
 0.896908
 0.913037
 0.934834

 STD DEV
 0.001905
 0.001826
 0.001752
 0.001624
 0.001422

TOTAL MSE: 491.56E-04

MSE

DISTRIBUTION: BERNOULLI-EX PONENTIAL

THEORETICAL PERCENTILES (P)

ESTINATES: 0.75 0.80 0.85 0.90 0.95

MEAN 0.738072 0.795951 0.840430 0.855563 0.950685

STD DEV 0.002533 0.002322 0.002110 0.001755 0.001248

MSE 0.002132 0.002338 0.002267 0.002224 0.001327

TOTAL MSE: 102.88E-04

DISTRIBUTION: BERNOULLI-LOGNORMAL

THEORETICAL PERCENTILES (P)

ESTINATES: 0.75 0.80 0.85 0.90 0.95

MEAN 0.749344 0.809159 0.849391 0.903886 0.948263

STD DEV 0.002497 0.002264 0.002061 0.001698 0.001276

MSE 0.001456 0.001751 0.001730 0.001866 0.001258

TOTAL MSE: 80.60E-04

MEDIUM DEMAND RANGE: 1.0 < D < 20.0 PER YEAR

DISTRIBUTION: BERNOULLI-LOGISTIC

THEORETICAL PERCENTILES (P)

 ESTINATES:
 0.75
 0.80
 0.85
 0.90
 0.95

 MEAN
 0.760006
 0.821542
 0.864176
 0.916219
 0.955416

 STD DEV
 0.002461
 0.002206
 0.001974
 0.001596
 0.001189

 MSE
 0.002256
 0.002499
 0.002304
 0.002030
 0.001241

TOTAL MSE: 103.30E-04

HIGH DEMAND RANGE: 20.0 < D PER YEAR

DISTRIBUTION: POISSON

THE ORETICAL PERCENTILES (P)

ESTINATES: 0.75 0.80 0.85 0.90 0.95

MEAN 0.689018 0.730300 0.753320 0.780038 0.800697

STD DEV 0.003534 0.003388 0.003291 0.003162 0.003050

MSE 0.024843 0.027146 0.033935 0.042154 0.051388

TOTAL MSE: 1794.66E-04

DISTRIBUTION: <u>NEGATI VE BIN OMIA L</u>

THEORETICAL PERCENTILES (P)

ESTINATES: 0.75 0.80 0.85 0.90 0.95

MEAN 0.724173 0.747130 0.791313 0.848041 0.896526

STD DEV 0.003412 0.003318 0.003102 0.002740 0.002325

MSE 0.003047 0.024647 0.026816 0.029773 0.031637

TOTAL MSE: 1159.20E-04

DISTRIBUTION: NORMAL

THEORETICAL PERCENTILES (P)

ESTIMATES: 0.75 0.80 0.85 0.90 0.95

MEAN 0.850264 0.871100 0.890154 0.910670 0.934248

STD DEV 0.002724 0.002558 0.002387 0.002177 0.001892

MSE 0.016622 0.010312 0.005815 0.003155 0.002227

TOTAL MSE: 381.32E-04

HIGH DEMAND RANGE: 20.0 < D PER YEAR

DISTRIBUTION: EXPONENTIAL

THEORETICAL PERCENTILES (P)

ESTINATES: 0.75 0.80 0.85 0.90 0.95

MEAN 0.784610 0.814275 0.846685 0.881207 0.918702

STD DEV 0.003138 0.002969 0.002750 0.002470 0.002086

MSE 0.009534 0.006885 0.005219 0.004384 0.003800

TOTAL MSE: 298.21E-04

DISTRIBUTION: LOGNORMAL

THEORETICAL PERCENTILES (P)

ESTIMATES: 0.75 0.80 0.85 0.90 0.95

MEAN 0.855867 0.886448 0.918614 0.949144 0.978288

STD DEV 0.002681 0.002422 0.002087 0.001677 0.001113

MSE 0.019028 0.013031 0.008113 0.004389 0.001639

TOTAL MSE: 462.00E-04

DISTRIBUTION: LAPLACE

THEORETICAL PERCENTILES (P)

ESTINATES: 0.75 0.80 0.85 0.90 0.95

MEAN 0.843416 0.863600 0.885612 0.907473 0.934956

STD DEV 0.002774 0.002620 0.002430 0.002212 0.001883

MSE 0.015775 0.009709 0.005680 0.003248 0.002167

TOTAL MSE: 365.79E-04

HIGH DEMAND RANGE: 20.0 < D PER YEAR

DISTRIBUTION: LOGISTIC

THEORETICAL PERCENTILES (P)

 ESTINATES:
 0.75
 0.80
 0.85
 0.90
 0.95

 MEAN
 0.822132
 0.846791
 0.871709
 0.900110
 0.933755

 STD DEV
 0.002919
 0.002750
 0.002553
 0.002289
 0.001899

MSE 0.013721 0.008841 0.005633 0.003523 0.002259

TOTAL MSE: 339.76E-04

DISTRIBUTION: <u>BERNOULLI-EX PONENTIAL</u>

THEORETICAL PERCENTILES (P)

 ESTIMATES:
 0.75
 0.80
 0.85
 0.90
 0.95

 MEAN
 0.759754
 0.816600
 0.867492
 0.914225
 0.955101

 STD DEV
 0.003261
 0.002954
 0.002588
 0.002138
 0.001581

 MSE
 0.005828
 0.005034
 0.003977
 0.002618
 0.001432

TOTAL MSE: 188.90E-04

DISTRIBUTION: BERNOULLI-LOGNORMAL

THEORETICAL PERCENTILES (P)

ESTIMATES: 0.75 0.80 0.85 0.90 0.95

MEAN 0.745078 0.797614 0.847684 0.901963 0.953670

STD DEV 0.003327 0.003067 0.002743 0.002270 0.001605

MSE 0.004768 0.004403 0.003632 0.002613 0.001409

TOTAL MSE: 168.25E-04

HIGH DEMAND RANGE: 20.0 < D PER YEAR

DISTRIBUTION: BERNOULLI-LOGISTIC

THE ORETICAL PERCENTILES (P)

 ESTIMATES:
 0.75
 0.80
 0.85
 0.90
 0.95

 MEAN
 0.828539
 0.864722
 0.892571
 0.921326
 0.947036

 STD DEV
 0.002877
 0.002611
 0.002364
 0.002055
 0.001710

MSE 0.012517 0.008862 0.005485 0.003020 0.001538

TOTAL MSE: 314.23E-04

APPENDIX C

REPAIRABLE ITEM TABULATED RESULTS

40 REPETITIONS FOR EACH OF 137 PSEUDO SAMPLES

LOW DEMAND RANGE: 0.0 < D < 1.0 PER YEAR

DISTRIBUTION: POISSON

THEORETICAL PERCENTILES (P)

ESTIMATES: 0.75 0.80 0.85 0.90 0.95

MEAN 0.750000 0.812496 0.853613 0.912594 0.955936

STD DEV 0.005849 0.005273 0.004775 0.003815 0.002772

MSE 0.0 0.000156 0.000019 0.000311 0.000099

TOTAL MSE: 5.86E-04

DISTRIBUTION: <u>NEGATI VE BIN OMIAL</u>

THEORETICAL PERCENTILES (P)

ESTIMATES: 0.75 0.80 0.85 0.90 0.95

MEAN 0.750000 0.812496 0.853613 0.912594 0.950753

STD DEV 0.005849 0.005273 0.004775 0.003815 0.002923

MSE 0.0 0.000156 0.000019 0.000311 0.000270

TOTAL MSE: 7.57E-04

LOW DEMAND RANGE: 0.0 < D < 1.0 PER YEAR

DISTRIBUTION: NORMAL

THEORETICAL PERCENTILES (P)

ESTIMATES: 0.75 0.80 0.85 0.90 0.95

MEAN 0.949164 0.949164 0.949164 0.949164 0.949164

STD DEV 0.002967 0.002967 0.002967 0.002967

MSE 0.040918 0.023465 0.011016 0.003568 0.001118

TOTAL MSE: 800.84E-04

DISTRIBUTION: EXPONENTIAL

THEORETICAL PERCENTILES (P)

ESTINATES: 0.75 0.80 0.85 0.90 0.95

MEAN 0.949164 0.949164 0.949164 0.949164

STD DEV 0.002967 0.002967 0.002967 0.002967

MSE 0.040918 0.023465 0.011016 0.003568 0.001118

TOTAL MSE: 800.84E-04

DISTRIBUTION: LOGNORMAL

THEORETICAL PERCENTILES (P)

ESTIMATES: 0.75 0.80 0.85 0.90 0.95

MEAN 0.978874 0.991028 0.991028 1.000000 1.000000

STD DEV 0.001943 0.001274 0.00 1274 0.0 0.0

MSE 0.052955 0.036815 0.020201 0.009996 0.002500

TOTAL MSE: 1224.66E-04

LOW DEMAND RANGE: 0.0 < D < 1.0 PER YEAR

DISTRIBUTION: LAPLACE

THEORETICAL PERCENTILES (P)

ESTINATES: 0.75 0.80 0.85 0.90 0.95

MEAN 0.949164 0.949164 0.949164 0.949164 0.949164

STD DEV 0.002967 0.002967 0.002967 0.002967

MSE 0.040918 0.023465 0.011016 0.003568 0.001118

TOTAL MSE: 800.84E-04

DISTRIBUTION: LOGISTIC

THEORETICAL PERCENTILES (P)

ESTIMATES: 0.75 0.80 0.85 0.90 0.95

MEAN 0.949164 0.949164 0.949164 0.949164 0.949164

STD DEV 0.002967 0.002967 0.002967 0.002967

MSE 0.040918 0.023465 0.011016 0.003568 0.001118

TOTAL MSE: 800.84E-04

DISTRIBUTION: BERNOULLI-EX PONENTIAL

THEORETICAL PERCENTILES (P)

ESTIMATES: 0.75 0.80 0.85 0.90 0.95

MEAN 0.750000 0.812496 0.853613 0.912594 0.942635

STD DEV 0.005849 0.005273 0.004775 0.003815 0.003141

MSE 0.0 0.000156 0.000019 0.000311 0.000804

TOTAL MSE: 12.91E-04

60

LOW DEMAND RANGE: 0.0 < D < 1.0 PER YEAR

DISTRIBUTION: BERNOULLI-LOGNORMAL

THEORETICAL PERCENTILES (P)

ESTINATES: 0.75 0.80 0.85 0.90 0.95

MEAN 0.750000 0.812496 0.853613 0.912594 0.942635

STD DEV 0.005849 0.005273 0.004775 0.003815 0.003141

MSE 0.0 0.000156 0.000019 0.000311 0.000804

TOTAL MSE: 12.91E-04

MSE

DISTRIBUTION: BERNOULLI-LOGISTIC

THEORETICAL PERCENTILES (P)

0.0 0.000156 0.000019 0.000311 0.000804

 ESTINATES:
 0.75
 0.80
 0.85
 0.90
 0.95

 MEAN
 0.750000
 0.812496
 0.853613
 0.912594
 0.942635

 STD DEV
 0.005849
 0.005273
 0.004775
 0.003815
 0.003141

TOTAL MSE: 12.91E-04

MEDIUM DEMAND RANGE: 1.0 < D < 20.0 PER YEAR

DISTRIBUTION: POISSON

THEORETICAL PERCENTILES (P)

ESTINATES: 0.75 0.80 0.85 0.90 0.95

MEAN 0.747034 0.806323 0.843928 0.894732 0.929457

STD DEV 0.001782 0.001620 0.001488 0.001258 0.001050

MSE 0.000238 0.000507 0.000582 0.001321 0.001836

TOTAL MSE: 44.84E-04

DISTRIBUTION: <u>NEGATI VE BINOMIA L</u>

THEORETICAL PERCENTILES (P)

 ESTIMATES:
 0.75
 0.80
 0.85
 0.90
 0.95

 MEAN
 0.744688
 0.804450
 0.843869
 0.900645
 0.944953

 STD DEV
 0.001788
 0.001626
 0.001488
 0.001227
 0.000935

 MSE
 0.000444
 0.000598
 0.000533
 0.000788
 0.000551

TOTAL MSE: 29.14E-04

DISTRIBUTION: NORMAL

THEORETICAL PERCENTILES (P)

ESTIMATES: 0.75 0.80 0.85 0.90 0.95

MEAN 0.861474 0.875334 0.890316 0.905783 0.927155

STD DEV 0.001416 0.001354 0.001281 0.001198 0.001066

MSE 0.019444 0.011363 0.006084 0.003600 0.002944

TOTAL MSE: 434.35E-04

MEDIUM DEMAND RANGE: 1.0 < D < 20.0 PER YEAR

DISTRIBUTION: EXPONENTIAL

THEORETICAL PERCENTILES (P)

 ESTINATES:
 0.75
 0.80
 0.85
 0.90
 0.95

 MEAN
 0.823217
 0.834022
 0.845365
 0.864271
 0.886389

 STD DEV
 0.001564
 0.001526
 0.001482
 0.001404
 0.001301

 MSE
 0.016435
 0.010140
 0.007542
 0.006691
 0.007993

TOTAL MSE: 488.02E-04

DISTRIBUTION: LOGNORMAL

THEORETICAL PERCENTILES (P)

 ESTINATES:
 0.75
 0.80
 0.85
 0.90
 0.95

 MEAN
 0.946618
 0.955351
 0.964288
 0.975138
 0.987135

 STD DEV
 0.000922
 0.000847
 0.000761
 0.000638
 0.000462

 MSE
 0.041761
 0.026454
 0.014803
 0.006692
 0.001890

TOTAL MSE: 916.00E-04

DISTRIBUTION: LAPLACE

THEORETICAL PERCENTILES (P)

ESTINATES: 0.75 0.80 0.85 0.90 0.95

MEAN 0.856232 0.870161 0.885855 0.902481 0.928262

STD DEV 0.001439 0.001378 0.001304 0.001216 0.001058

MSE 0.018823 0.011026 0.006113 0.003736 0.002851

TOTAL MSE: 425.48E-04

MEDIUM DEMAND RANGE: 1.0 < D < 20.0 PER YEAR

DISTRIBUTION: LOGISTIC

THEORETICAL PERCENTILES (P)

ESTIMATES: 0.75 0.80 0.85 0.90 0.95

MEAN 0.845409 0.858922 0.875792 0.896303 0.925823

STD DEV 0.001482 0.001427 0.001352 0.001250 0.001075

MSE 0.017690 0.010603 0.006269 0.004086 0.003093

TOTAL MSE: 417.42E-04

DISTRIBUTION: <u>BERNOULLI-EX PONENTIAL</u>

THEORETICAL PERCENTILES (P)

ESTIMATES: 0.75 0.80 0.85 0.90 0.95

MEAN 0.730065 0.787917 0.834508 0.893026 0.954267

STD DEV 0.001820 0.001676 0.001524 0.001267 0.000857

MSE 0.003437 0.003608 0.003449 0.003021 0.001465

TOTAL MSE: 149.79E-04

DISTRIBUTION: BERNOULLI-LOGNORMAL

THEORETICAL PERCENTILES (P)

ESTIMATES: 0.75 0.80 0.85 0.90 0.95

MEAN 0.750179 0.808666 0.852134 0.904194 0.949477

STD DEV 0.001775 0.001613 0.001455 0.001207 0.000898

MSE 0.002226 0.002681 0.002600 0.002327 0.001410

TOTAL MSE: 112.44E-04

MEDIUM DEMAND RANGE: 1.0 < D < 20.0 PER YEAR

DISTRIBUTION: BERNOULLI-LOGISTIC

THEORETICAL PERCENTILES (P)

 ESTIMATES:
 0.75
 0.80
 0.85
 0.90
 0.95

 MEAN
 0.762406
 0.822694
 0.866844
 0.915851
 0.953988

 STD DEV
 0.001745
 0.001566
 0.001393
 0.001138
 0.000859

 MSE
 0.003183
 0.003523
 0.003107
 0.002468
 0.001379

TOTAL MSE: 136.61E-04

HIGH DEMAND RANGE: 20.0 < D PER YEAR

DISTRIBUTION: POISSON

THEORETICAL PERCENTILES (P)

ESTINATES: 0.75 0.80 0.85 0.90 0.95

MEAN 0.695829 0.735554 0.762330 0.791447 0.821025

STD DEV 0.003855 0.003696 0.003567 0.003405 0.003212

MSE 0.022812 0.026569 0.032141 0.038638 0.044655

TOTAL MSE: 1648.16E-04

DISTRIBUTION: <u>NEGATI VE BINOMIA L</u>

THEORETICAL PERCENTILES (P)

ESTIMATES: 0.75 0.80 0.85 0.90 0.95

MEAN 0.722861 0.755975 0.799852 0.857560 0.904930

STD DEV 0.003751 0.003599 0.003353 0.002929 0.002458

MSE 0.005285 0.024724 0.026795 0.028699 0.030113

TOTAL MSE: 1156.16E-04

DISTRIBUTION: NORMAL

THEORETICAL PERCENTILES (P)

ESTIMATES: 0.75 0.80 0.85 0.90 0.95

MEAN 0.836334 0.859810 0.883941 0.905503 0.932035

STD DEV 0.003100 0.002909 0.002684 0.002451 0.002109

MSE 0.014669 0.009278 0.005429 0.003190 0.002319

TOTAL MSE: 348.85E-04

HIGH DEMAND RANGE: 20.0 < D PER YEAR

DISTRIBUTION: EXPONENTIAL

THEORETICAL PERCENTILES (P)

ESTINATES: 0.75 0.80 0.85 0.90 0.95

MEAN 0.780940 0.818187 0.856974 0.898153 0.935255

STD DEV 0.003466 0.003232 0.002934 0.002535 0.002062

MSE 0.009578 0.007296 0.005229 0.003830 0.002968

TOTAL MSE: 289.01E-04

DISTRIBUTION: LOGNORMAL

THEORETICAL PERCENTILES (P)

ESTIMATES: 0.75 0.80 0.85 0.90 0.95

MEAN 0.819119 0.855337 0.895522 0.933281 0.971445

STD DEV 0.003226 0.002948 0.002563 0.002091 0.001396

MSE 0.013003 0.008704 0.005985 0.093420 0.001454

TOTAL MSE: 325.65E-04

DISTRIBUTION: LAPLACE

THEORETICAL PERCENTILES (P)

ESTINATES: 0.75 0.80 0.85 0.90 0.95

MEAN 0.827652 0.85 2088 0.877334 0.902360 0.932870

STD DEV 0.003165 0.00 2975 0.00 2749 0.002487 0.00 2097

MSE 0.013659 0.008798 0.005346 0.003302 0.002267

TOTAL MSE: 333.71E-04

HIGH DEMAND RANGE: 20.0 < D PER YEAR

DISTRIBUTION: LOGISTIC

THEORETICAL PERCENTILES (P)

ESTIMATES: 0.75 0.80 0.85 0.90 0.95

MEAN 0.805812 0.833134 0.860882 0.892308 0.930748

STD DEV 0.003315 0.003125 0.002900 0.002598 0.002128

MSE 0.012232 0.008347 0.005666 0.003803 0.002397

TOTAL MSE: 324.44E-04

DISTRIBUTION: BERNOULLI-EX PONENTIAL

THEORETICAL PERCENTILES (P)

ESTIMATES: 0.75 0.80 0.85 0.90 0.95

MEAN 0.770942 0.829521 0.877192 0.921468 0.960362

STD DEV 0.003522 0.003151 0.002750 0.002254 0.001635

MSE 0.007108 0.005916 0.004548 0.003092 0.001516

TOTAL MSE: 221.80E-04

DISTRIBUTION: BERNOULLI-LOGNORMAL

THEORETICAL PERCENTILES (P)

ESTIMATES: 0.75 0.80 0.85 0.90 0.95

MEAN 0.746108 0.797150 0.847197 0.901039 0.953617

STD DEV 0.003647 0.003370 0.003015 0.002502 0.001762

MSE 0.005655 0.004764 0.003680 0.002809 0.001469

TOTAL MSE: 183.77E-04

HIGH DEMAND RANGE: 20.0 < D PER YEAR

DISTRIBUTION: <u>BERNOULLI-LOGISTIC</u>

THEORETICAL PERCENTILES (P)

 ESTINATES:
 0.75
 0.80
 0.85
 0.90
 0.95

 MEAN
 0.829834
 0.861163
 0.886755
 0.914062
 0.941856

 STD DEV
 0.003149
 0.002898
 0.002656
 0.002349
 0.001961

 MSE
 0.013074
 0.008963
 0.005495
 0.003143
 0.001722

TCTAL MSE: 323.98E-04

APPENDIX D

ESTIMATION OF LOGNORMAL MEAN AND VARIANCE FROM UNTRANSFORMED DATA

The usual method of estimating the sample mean and variance of a random sample assumed to come from a lognormal distribution is to take the log transform of the data and then compute the standard method of moments estimates. This is time consuming on a computer as the logarithm must be taken for each observation in the sample. Formulae to compute the mean and variance of the untransformed data from the mean and variance of the transformed data can be derived for the lognormal distribution.

If Y is distributed normal(μ_Y , σ_Y^2), then X is distributed lògnormal if Y = ln(X). The mean of X [Ref. 10] is expressed as:

$$\mu_{X} = e^{\mu_{Y} + \frac{1}{2}\sigma_{Y}^{2}} \tag{20}$$

and the variance as:

$$\sigma_{X}^{2} = e^{2(\mu_{Y} + \frac{1}{2}\sigma_{Y}^{2})} \left(e^{\sigma_{Y}^{2}} - 1\right).$$
 (21)

Equations (20) and (21) are the reverse of that required in this case since μ_y and σ_y^2 are obtained from the transformed

data. What is needed then, is to solve for μ_y and σ_y^2 in terms of μ_x and σ_x^2 . Substituting (20) into (21) results in:

$$\sigma_{\chi}^{2} = \mu_{\chi}^{2} \left(e^{\sigma_{\gamma}^{2}} - 1 \right) \tag{22}$$

which when solved for $e^{\sigma_y^2}$, taking logs and simplifying, gives the sclution of σ_y^2 as:

$$\sigma_{\gamma}^{2} = \ln\left(\frac{\sigma_{x}^{2} + \mu_{x}^{2}}{\mu_{x}^{2}}\right). \tag{23}$$

Substituting (23) back into the log of (20), solving for μ_y and simplifying gives the solution of μ_y as:

$$\mu_{y} = \ln\left(\frac{\mu_{x}^{2}}{\sqrt{\mu_{x}^{2} + \sigma_{x}^{2}}}\right). \tag{24}$$

Thus the mean and variance of the transformed data may be estimated from the sample mean and variance of the untransformed data reducing significantly the computational requirements.

APPENDIX_E

DATA RECORD LAYOUT

5A Master Input Pile; 600 Characters Per Record, 10 Records Per Block, Pixed Length

CH POS	-	2-31	4-12	13-22	23-32	33-42	43-52	53	94	
	+				Ī					_
<u>-</u>	RECORDI COG		NIIN	REPLACE-	COST	SET	REPAIR	PROCUREMENT	NEWLY	
A	TYPE	_	_	MENT	To	UP	SET UP	METHOD	PROVISIONED	_
	("1")			PRICE	REPAIR	COST	COST	CODE	INDICATOR	
~	- •	-		1 (808)	(B055A)	(8028)	(B055A)	(D025E)	(B067A)	
PICTURE	-	2	6	8.2	8.2	8.2	8.2	-	-	

CH POS	55	95	57	58	59	09
0	DEMAND	GH D DEMA	HIGH REPLACE-	PROGRAM RELATED	REPAIRABLE!	AUTOMATIC REPAIR CYCLE
E 4	(80678)	INDICATOR (B067C)	INDICATOR (B067D)	INDICATOR (B067E)	INDICATOR (B067F)	INDICATOR (B067G)
PICTURE	1	1	1	1	1 1	

CH POS	61	62-65	89-99	69-71	72-74	75-77	78-80
OAHA	NAVY REPORTING REPAIRABLE INDICATOR	PROCURE- HENT LEADTIME (B0 11A)	PROCURE- PROCURE- HENT HENT LEAD- LEADTIME TIME M.A.). (B011A) (B011B)	REPAIR SURVIVAL RATE (P009)	REPAIR SURVIVAL RATE H.A.D.	WEAR- OUT RATE (FOO7)	ITEM ESSEN- TIALITY (C008C)
PICTURE		2.2	2.1	1.2	1.2	1.2	.3

CH POS	POS 81-83	84-86	87-96	97-106	107-116	117-126	127-136
Q	H	OBSO	SYSTEM	SYSTEM	SYSTEM OVER-		6-3
⋖	LIPE	LESCENCE	DEMAND	DEHAND	HAUL DERAND	HAUL DERAND	CASS RETURN
H	1 (C028) 1	RATE	AVERAGE	H. A. D. I	AVERAGE	H. A. D.	AVERAGE
⋖		(B057)	(B022) ((4019) {	(B022A)	(A0 19A)	(B022B)
PICTURE	1.2	1.2	5.5	5.5	5.5	5.5	5.5

CH POS	POS 137-146	147-152 153-157	153-157	158-167	168-177	178	186-193
DAHA	SYSTEM CAR-I CASS RETURN M.A.D.	SYSTEM REQUISITION AVERAGE (A023B)	UNIT PACK (C021B)	ACQUISITION QUARTERLY HAR DEMAND RESERVE FORECAST (8028C) (8074)	QUARTERLYI DEMAND FORECAST (B074)	REPAIR LEVEL (B0 19B)	PAIR ANTIT 021A)
PICTURE	5.5	4.2	5	10	8.2	8	8

CH POS	194-192	197-199	200-202	203-205	206-208
A	NOMBER (MANY MONREPORT-INA	Y NONREPORT - NAVY NONREPORT - NAVY REPORTING	NAVY REPORTING	NAVY REPORTING
4	POLICY	ING/COMMERCIAL	ING/COMMERCIAL	REPAIR IN	REPAIR IN PRO-
6	RECEIVER	REPAIR TAT	REPAIR M.A.D.	PROCESS TIME	CESS TIME M.A.D.
4	ACTIVITIES	(B012)	(B012B)	(B012C)	(B012D)
PICTURE	3	1.2	2.1	1.2	2.1
	•				

	-			15 (5
	ALUES	11 P		51
	AINTENANCE PROGRAM VALUES	P 1 P 1	-	5 15
302	PROG	16 16 17		1 2
233-302	NCE	4 L		51
	FENA	al al al		5 5
	MAIN	<u> </u>		2 - 6
	2	_ B _ E		1 5 1
		11 21 31 41		2
		٠ ٣ =		5 .
	├ - -	ATI		5
223-232	SYSTEM	THE REPAIR T	3H	8.2
1213-222	SYSTEM	LEAD OF	(B023 D)	8.2
12	REPAIR PROBLEM	TAT		2.2
CH POS	Q 4			PICTURE

					303	303-372	8					373-379	380-385	386
۵۰			OVER	HAUL	PRO	PROSRAM	RHAUL PROSRAM VALUES	LUES				SYSTEM	SYSTEM	DOP
4 6 4	P P	1 P P	4 P	1 d	P - P	6 - 8 - 8 - 8	16 16	P P P P P P P P P P	P 12	1 P 1 3	P 141	IN (QUANTITY (CATOR
I ICTURE 15	15 15	15 15	2	15 15	5 5	15	- 2	15	12	2	15	į	9	1

D MAXIMUM ON-HAND ON-HAND ON-HAND ON-HAND NOT-FIT H A INDUCTION WHO LESALE NAS RETAIL FOR CONDITION T QUANTITY CONUS ALAMEDA CONUS CECIL OVERSEAS ISSUE ON-HAND A (8095) TIRS TIRS TIRS ON-HAND PICTURE 3 7 7 7 7 7 7 7 7 7	CH POS	H POS 387-390	1 391-397	1398-4041	1-397 398-404 405-411 412-418 419-425	412-418		426-432	433-439
T (QUANTITY CONUS ALAMEDA CONUS CECIL OVERSEAS ISSUE A (8095) TIRS TIRS FIELD TIRS ON-HAND ICTURE 3 7 7 7 7 7 7 7 7 7	a	MAXIBUM	ON-HAND	ON-HAND	i	ON-HAND!	ON-HAND	NOT-FIT	æ
I (8095) TIRS TIRS FIELD TIRS ON-HAND ICTURE 3 7 7 7 7 7	_	DUCTION	LESALE	ISTR	RETAIL		RETAIL (FOR	COMPLETON
ICTURE 3 1 7 1 7 1 7 1	- -	QUARTITI	TRS	ALABEDA	TIRS	FIELD	TIRS	ON-HAND	
ICTURE				+	+	+	+		
	\vdash	m	_	· ·			_	>	_

CH POS	9 11 - 011	447-453	091-1151	191-191	1 468-474
a	OTAL RESERVA-	ZGS RESERVATIONS	TOTAL	ZG5 RESERVA-	TOTAL RESER-
- V	A TCHA LY SNO	AT WHOLESALE	ESERVATIONS	TIONS AT NAS	VATIONS AT
- H	SALE CONUS TIRS!	CONUS TIRS	AT NAS ALAMEDA	ALAMEDA	RETAIL CONUS
A	(A0 13A)	(A013)	(A013A)	(A013)	TIRS (A013A)
PICTURE	7	7	7	7	7

CH POS	-481	4 82-	561-681		503-209
0	G5 RESERV	-	ZGS RESERVA-	TOTAL RESERVA-	265
~ ~	ITIONS AT RE-	TIONS AT NAS	ITIONS AT NASITIONS	Y	AT
	TAIL CONUS	CECIL FIELD	CECIT FIELD !	OVERSEAS TIRS	SEAS TIRS
4	TIRS (A013)	(A013A)	(A013)	(A013A)	(A013)
PICTURE	7	7	7	7	7

CH POS	510-512	513	514-520 521-527 528-534	521-527	528-534	535-544	545-554
0	NAS	TYPE	YPE (PROTECTED)	100d	OUTFIT-	COUTFIT- BRROR TERM	ERROR TERM
. 	ATION	INDI	FION REQ-	REQ- VATIONS RESER-	RESER- FIR VATIONS TER	S	SECOND e2
PICTURE	3	1	7		7	\$5.5	\$5.5

1009		
97-	ANIGRO	3
296	BLANK	-
586-59	STANDARD PRICE (B053)	8.2
75	BL ANKS	11 1
565-574	R I ANC S I GHA Q UARE	5.5
1995-555	EXPECTEDI BRROR VALUE - E(X)	\$5.5
CH POS	OAHA	PICTURE

5A Demand Trailers; 600 Characters Per Record, 10 Records Per Block, Fixed Length

CH POS	-	7	m	#	'n	16-9	6-9110-13	14	15	16	17
0 < 6	RECORDI TYPE (ENTRY T POINT DE	TYPE I B	DEMAND	PRIORITY DAY ANOUNT LEVEL POINT DEMAND	DAY	AHOUNT	BOLEVEL	ENTRY POINT		RECUR- RENG DEMAND
4										1	CODE
PICTURE	-	-	-		-	=	3	-	-	-	11

CH POS	18	19-20	23-26	27	587	588	589	290
OAHA	PRIORITY	DAY	ANOUNT	BOLEVEL	ENTRY POINT CODE	TYPE DEMAND CODE	RECUR- RING DEMAND	PRIORITY
PICTURE	1	#	ή	-	-	-	-	1

009	0.	-
599	BOLEVEL	-
5 95-598	AMOUNT	t
591-594	DAY	#
CH POS	OWHW	PICTURE

APPENDIX P

FORTRAN PROGRAMS

THIS PROGRAM IS DESIGNED TO TAKE A 1 IN PREQ SAMPLE FROM THE RETRIEVE RECORDS, ONLY THE RECORD/SUBRECORD INDICATOR IS COPIED. THE REMAINING DATA ELEMENTS REPRESENTING INFORMATION NOT USED IN THIS ANALYSIS ARE DISCARDED. ALL DEMAND SUBRECORDS FOR EACH BY SETTING THE VALUES OF DEVICE AND COPIES THE INPUT RECORDS TO A TRANSFER DISK THAT IS ACCESSIBLE TO THE VM SYSTEM. THE MAIN DATA RECORDS AND ONLY A PORTION OF THE RAW DATA FOR TRANSFER. IN THIS WAY, INDEPENDENT SETS OF DATA COULD BE EVALUATED TO VERIFY THE MYSTOWN PROGRAM READS THE RAW DATA FROM THE MASS STORAGE THE VARIABLES START AND PREQ, THE USER IS ABLE TO SELECT SUBRECORDS ARE TREATED DIPPERENTLY IN THAT FOR THE MAIN -- CHARACTER ARRAY USED TO TRANSFER DATA //YOUNT\$\$A JOB (1642,0045), "MARK YOUNT", CLASS=B, MSGCLASS=Z USE MVSGET EXEC TO HSS.S1642.THESIS1 FOR 1R DATA AND MSS.S1642.THESIS2 DATA. THE FILEDEF FOR FT01F001 MUST BE CHANGED FOR PMSO 5A SIMULATOR ASO DEMAND DATA STORED ON MAIN RECORD ARE COPIED UNALTERED. WHICHEVER DATA SET IS REQUIRED. DEFINITION OF VARIABLES: THE SAMPLE FROM MVS004. POWER OF THE PROCEDURE. EXEC PORTICLG //FORT. SYSIN DD @ A (599) の本語 のをは の機能 を登り なない の数の # C # * * CCC # C のなり ない。 のなり # 3 CAR ##0 C S # 5

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                                                                                                                                                         经存储的股票 经存储的 医骨部骨的 医小骨的 经公司的经济的 医克勒特氏 医多种性 医多种性 医多种性 医多种性 医多种性 医多种性 医多种性 医克勒特氏病 计可以分析计划
WRITTEN TO OUTPUT FILE AS END OF FILE INDICATOR
                                                                                                                                                                                                                                                                                                                                                                                                                                         READ AND TRANSPER TO MVS 004 DESIRED RECORDS AND SUBRECORDS
                                                                                                                      TO COPY BUTIRE PILE TO MVSOO4, SET START = 0 AND PRRQ =
                                                                                                                                                                                                                                                                                                                                                                                                        IF (.NOT. ((N.EQ.1).AND. (MOD (IN+1, FREQ).EQ.START))) GOTO 40
                                                                                                                                                                                           START,
                                                                                    -- RECORD NUMBER OF FIRST RECORD TO READ
                                                 1 = RECORD/2 = SUBRECORD INDICATOR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   READ(1,810,END=80) N, (A(I),I=1,599)
                                                                   COUNT OF RECORDS WRITTEN
                                                                                                                                                                                                                                              SET PREQ TO DESIRED SAMPLING PREQUENCY.
                                                                                                                                                                                          FREQ.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               READ (1,810, END =80) N, (A(I), I=1,599)
                                COUNT OF RECORDS READ
                                                                                                                                                                                                                                                                                                                 SET START TO DESIRED PIRST LINE ITEM.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  WRITE(2,810) N, (A(I), I=1,599)
                SAMPLING PREQUENCY
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 TP (.NOT.(N .EQ. 2)) GOTO 30
                                                                                                                                                                                           N,
IN/0/,
                                                                                                                                                                                                                                                                                                                                                                    READ(1,800, END=80)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              WRITE (2, 800) N
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             00T = 00T +
                                                                                                                                                                                                                                                                                                                                                                                                                                                                            L + NI = NI
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                CONTINUE
                                                                                                                                                                                          A (599),
                                                                                                                                                                                                            EOF/0/,
                                                                                                                                                                                                                                                                                                                                                     START = 0
                                                                                                                                                                          INTEGERA
                                                                                                                                                                                                                                                                                                                                                                                       CONTINUE
                                                                                     STABT
                PREQ
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      GOTO
                                                                                                                                                                                                                                                                                 FREQ =
                                                                   TOO
                                                                                                                       NOTE:
                                                                                                                     ##O
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IN AND', IS, ' RECORDS
                                                                                                                                                                                                                                                                                                                                                                                        FORMAT(11,8 (75A1))
FORMAT(/'STARTING AT RECORD ',13,' AND SKIPPING EVERY ',13,
' RECORDS',/,15,' RECORDS WERE READ IN AND',15,' RECORDS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            DCB= (RECFM=FB, LREC L=600, BLKS IZE=6000), SPACE= (CYL, (4, 1)),
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             //GO.FT01F001 DD DISP=SHR,DSN=MSS.S1642.THESIS1
//GO.FT02F001 DD UNIT=3350,VOL=SER=MVS004,DISP=(NEW,KEEP)
                                                               SKIP BY UNHANTED RECORDS AND SUBRECORDS
                                                                                                                                                9
                                                                                                                                                                                                                                                                                                                                              WRITE (2,820) START, FREQ, IN, OUT
                                                                                                                                             IF (.NOT.(N .EQ. 2)) GOTO
READ(1,800,END=80) N
                                                                                                                                                                                                                                                                               MARKER
                                                                                                            READ (1,800, END =80)
                                                                                                                                                                                                                                                                                                                                                                                                                            RECORDS', /, I5, '
                                                                                                                                                                                                                                                                              WRITE END OF FILE
                                                                                                                                                                                                                                                                                                              WRITE (2,800) BOP
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              DSN=S1642.OUTPUT
                                                                                                                                                                                                                                                                                                                                -
                                                                                                IN = IN + 1
                                                                                                                                                                                                                                                                                                                               PREQ = PREQ
                                                                                                                              CONTINUE
 CONTINUE
                                                                                                                                                                                               CONTINUE
                                                                                                                                                                              GO TO 50
                                                                                                                                                                                                                                                                                                                                                                               FIRMT (I1)
                                CONTINUE
                                                                                                                                                                                                               CONTINUE
                                                                                                                                                                                                                                               CONTINUE
               GOTO 70
                                                                                                                                                                                                                                Goro 10
                                                                                                                                                                                                                                                                                                                                                                STOP
                                                                                                                                                                                                                                                                                                                                                                                                                                                                END
                                                                                                                                                                                                                                                                                                                                                                                              8 10
8 20
30
                                                                                                                               50
                                                                                                                                                                                               09
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,我们的人们的人们的人们的,我们的人们的人们的人们的人们的,我们们的人们的人们的人们的人们的人们的人们的人们的人们的人们的人们的人们的人们的人		SIS IS THE MAIN PROGRAM FOR TH	T FUNCTIONS AS A CONTROL OVER TH	BEING EVALUATED BY CHECKING PARAMETERS RETURNED BY	ROUTINES. IF THE	ITS, THE ENTIRE SAMPLE IS DISCARDED BEFOR	ING. THE PARAMETERS CHECKED ARE	1. NUMBER OF NON-ZERO OBSERVATIONS GREATER	. STANDARD DEVIATION OF ANY DEMAND SERIES	HE SAMPLES ARE ALSO CATEGORIZED INTO LOW	IUMBER I	AT		DEFINITIONS OF VARIABLES:		AN FLOAT OF NBR	REAKPOINTS OF	-	UMERIC CALENDA	LOGICAL TEST FOR ERRORS IN STAT	RST LOGICAL VARIABLE TRUE ONLY	DISTRIBUTION PERCENTILES TO TES	HR HOUR	D CATEGORY FOR SAMPL	CUNT OF SAMPLES IN EACH DEMAND C	T DSRN FOR TERMINAL	K2 DSRN OF 1	IER RETURN CODE PROM STATS SUBROUTINE	NT DSRN OF	CONTROL PARAMETER FOR P	ISEED SEED FOR RANDOM NUMBER GENERATOR USED IN SAMPLE	J DO INDEX FOR GENERAL USE	MI HINUTES	MO NUMERIC MONTH OF YEAR	HODELS NUMBER OF MODELS TO STUDY
C###	# C	の数数	Catta	## ()	C C C C C C C C C C C C C C C C C C C	#	S C C	# * *	Ç Ç	# U	Cot	# * *	660	64 0	を兼り	## ()	9	₩	COS	Š U	の物質	(* ()	₽	\$ ₩	\$ \$ 0	の存在	Crath	₩ ₩ U	の数の	S T T T	C#C	の書か	COB	C#D	\$¢ C

0 0 0 # 0 0	# (B ·	& #	4 4	ű #	45 45	작 #	E.	ë H	⇔	찬 중	⊕	₩ #	かけ	ű.	찬 분	Či Š	# &	산 상	승 · 참	e G	ŭ G	₩ ₩	外语	ë ∯	ర త	&	€. Š	长	<u>්</u>	4	ර ජ ට ම	þ Þ
CHARACTER MONTHS OF THE YZAR MEAN SQUARED ERROR OF PREDICTED VS. ACTUAL PERCENTILE	AMPLE MEAN OF EACH GROUP OF OBSERVATI	OF DEMAND OBSERVATIONS TO TEST	P DEMAND OBSERVATION	1) ALWAYS EQUALS NBR	OF SAMPLE PERCENTILES TO	EMS	NUMBER OF PSEUDO SAMPLE REPETITIONS	OF DEMAND OBSERVATIONS	1. BAH OBSERVATIONS APTER REMOVING NEGATIVES	2. NON-ZERO DEMAND OBSERVATIONS	NON-ZERO DEMAND	RO DEMAND	COUNTER FOR ACCUMULATING PERCENTILE ESTIMATES		SAMPLE STANDARD DEVIATION OF EACH DEMAND GROUP	EACH PROBABILIT	BY S	TWO DIGIT VALUE OF YEAR		I RED:		NITIAL PILE DEPINITIONS	H DATA FROM DISK AND CRE	OF THREE DEMAND OBSERVATIONS AS FOLLOWS:	DATA	-ZERO OBSERVATIONS	3. LOG OF NON-ZERO OBSERVATIONS	NDARD DEVIATIONS OF AE	A PROBABILITY, COMPUTES THE	ISTRIBUTION INVERS	ENERATES PSEUDO SAMPLES AND TE	THE X VALUE COMPUTED IN XINV. ACCUMULATES PERSONITI SICCES AND AVERAGE MEAN SOMARE PERSOR	LI SUCCESS AND AVERAGE DEAN SQUARE
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HONTH MSE	D W		NB ROBS		NPTILE	NR ECD	NREPS	OBS				Q.	PH AT	သင	STDV	×		YR		SUBROUTINES		OPEN	INITAL					TSTATS	XI NA		SAMPLE		
\$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$	の事件	# # U	Cata	Ctate	CERT	\$ \$	を登し	# C	COS	C##C	€ E E E E	の数数	STATE OF	Cotto	CERT	ななり	の存在	の存む	Cata	の事件	の存在	CES	S S S S S S S S S S S S S S S S S S S	はない	COS	C.	Carre	C##	S C	C Marie	C#3	10 to	ر د د

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                                          PHAT(3,10,5)/150*0.0/,
PX(5)/0.75,0.80,0.85,0.90,0.95/
  AND YEAR PROM SYSTEM
                                                                                                                                                          MONTH (12) / JAN , 'FEB', MAR'
                                                                                                                                           NBR DEL/0/
                                                                                                                                                                       'APR', 'MAY', 'JUN', 'JUL', 'AUG', 'SEP', 'OCT', 'NOV', 'DEC'/
                                                                                                                              NBROBS (3)
                                                                                                                                                                                                                                                                                                                    IPRINT,
                                                                                                                NRECD,
                                                                                                 IER,
                                                                                                                               IC (3) /3¢0/,
                                                                                                                                                                                                                                                                                                                                                                                                                                                   CALL INITAL (FIRST, NBR, OBS, NBROBS, NBRNEG, 880)
                                                                                                                                                                                                                                 OBS (48,3),
                                                                                                                                                                                                                 STDV (3),
                                                                                                                NBR/48/.
                                                                                                                                                                                                                                                                                                                   ICNOUT,
-- GETS TIME AND MONTH, DAY
-- GENERATES OUTPUT REPORT
                                                                                                 IDSK2,
                                                                                                                                                                                                                               X(10,5),
HSE(3,10,5)/150@0.0/,
CAT(4)/0.0,1.0,20.0,9999.99/,
                                                                                                                                                                                                                                                                                         FIRST/. TRUE./
                                                                                                                                            MODELS/10/,
                                                                                                                                                          NBRNEG/0/,
                                                                                                                                                                                                                                                                                                                                                                             READ (IDSK2, f) NRECD, NREPS
                                                                                                                                                                                                                                                                                                                    ICONIN,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                              P = FLOAT (NBROBS(2)) / AN
                                                                                                                              NREPS,
                                                                                                                I PRT,
                                                                                                                                                                                                                                                                                                                                                                                       CAT(2) = CAT(2) / 12.0

CAT(3) = CAT(3) / 12.0
                                                                                                                                                                                                                                                                                                                                                 CALL OPEN ("THESIS")
                                                                                                                                            ISEED/392746/,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                  FIRST = . PALSE.
                                                                                                                                                                                                                                                                                                                                                             IDSK2 = IDSK(2)
                                                                                                                                                                                                                                                                                                                                                                                                                     AN = PLOAT (NBR)
                                                                                                                                                                                                                                                                                                      COMMON /PILES/
                                                                                                                              NPTILE/5/
                                                                                                                                                                                                                                                                                                                                  IDSK (30)
                                                                                                                IPRINT,
                                                                                                                                                           ICNOUT,
  DATINE
             OUTPUT
                                                                                                                                                                                                                  HO (3),
                                                                                                                                                                                                                                                                          LOGICAL*1
                                                         INTEGERAG
                                                                                                                                                                                                                                                                                          ERROR,
                                                                                                                                                                                                                                                                                                                                                                                                                                     CONTINUE
                                                                                                 IDSK,
                                                                                                                                                                                                                                                                                                                    IPRT,
                                                                                                                                                                                       REALWH
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RETURN BASIC STATISTICS FOR EACH GROUP OF OBSERVATIONS

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                                                                                      SKIP ENTIRE SAMPLE IF TOO SMALL OR STANDARD DEVIATION EQUALS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           BERNOULLI SUCCESS ES AND THE AVERAGE MEAN SQUARED ERROR OF
                                                                                                                                                              NU(2), STDV(2), P
NU(3), STDV(3), NBROBS(3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                               CONDUCT RESAMPLING PROCEDURE RETURNING THE NUMBER OF
                            CALL TSTATS (0BS(1,J), NBRJBS(J), MU(J), STDV(J), IER) IF (IER .NE. 0) ERROR = .TRUE.
                                                                                                                                                                                                                                                                                                                                                                                                                     COMPUTE LOCATION OF EACH PERCENTILE FOR ALL HODELS.
                                                                                                                                                MU (1), STDV (1)
                                                                                                                                                                                                          BY OVERALL MEAN
                                                                                                                                                                                                                                                                                                                                                                                                                                                  CALL XINV (P, MU, ST DV, FX, MODELS, NPTILE, X, IER)
                                                                                                                                                              WRITE (IPRINT, 610)
WRITE (IPRINT, 620)
                                                                                                                                               WRITE (IPRINT, 600)
                                                                                                                                                                                                                                                                                                 .GT. CAT(3) GOTO 40
                                                                                                                                                                                                                                       GOTO 30
                                                                                                                                                                                                          DIVIDE INTO DEMAND CATEGORIES
                                                                                                                   = NBRDEL +
                                                                                                                                                                                                                                       .GT. CAT(2))
                                                                                                                                GOTO 70
                                                                                                                   NBRDEL
                                                                                                                                                                                                                                                                                                                                                                                         IC(I) = IC(I) +
= . FALSE.
                                                                                                                                                               (IPRT .GE.
                                                                                                                                                IPRT GE.
              J=1,3
                                                                                                                   (ERROR)
                                                                                                                                 (ERROR)
                                                                                                                                                                                                                                                                                                 IP (HU(1)
                                                                                                                                                                            (I PRT
                                                                                                                                                                                                                                       (HU (1)
                                                         CONTINUE
                                                                                                                                                                                                                                                                                  CONTINUE
                                                                                                                                                                                                                                                                                                                                             CONTINUE
                                                                                                                                                                                                                                                                                                                                                                          CONTINUE
                                                                                                                                                                                                                                                                    GOTO 50
                                                                                                                                                                                                                                                                                                                             GOTO 50
              DO 20
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            MODEL.
ERROR
                                                        2000
                                                                                                                                                                                                                                                                                  30
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.-NUMBER OF SAMPLES DELETED BY POOR STATISTICS: ',13,/,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                RECORDS ASSIGNED AS MEDIUM DEMAND'/,
                                                                                                                                                                                                                                                                                                                                                                                                         SAMPLE STANDARD DEVIATION:
                                                                                                                                                                                                                                                                                                                                                                                                                                                           SAMPLE STANDARD DEVIATION:
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            SAMPLE STANDARD DEVIATION:
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       RECORDS ASSIGNED AS LOW DEMAND'/,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         RECORDS ASSIGNED AS HIGH DEMAND.)
                       CALL SAMPLE (IS EED, OBS, NBR, I, MODELS, NPTILE, X, PX, PHAT, MSE)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   PROBABILITY OF A NON-ZERO OBSERVATION: ", F10.8)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                FORMAT ("OREPORT GENERATED AT ", IZ,": ", IZ,": ", IZ," ON ",
                                                                                                                                                                                                                                                                                                                                                       CALL OUTPUT (MODELS, NPTILE, NREPS, PX, IC, PHAT, MSE, CAT)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            ONUMBER OF SAMPLES WITH NEGATIVE DEMANDS:
                                                                                                                                                                                                                                                     NBRDEL, NBRNEG, (IC (I), I=1,3)
                                                                                                                                                                                                                                                                              NBRDEL, NBRNEG, (IC(I), I=1,3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   NUMBER OF NON-ZERO OBSERVATIONS:
                                                                                                                                                                                                                                                                                                       HR, HI, SC, DY, MONTH (MO), YR
                                                                                                                                                                                                                                                                                                                                HR, MI, SC, DY, MONTH (MO), YR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            FORMAT ("1", 20x, "SUMMARY RUN STATISTICS", /,
                                                                                               IF (IC(1)+IC(2)+IC(3) .LT. NRECD) GOTO 10
                                                                                                                                                                                                                             CALL DATINE (YR, NO, DY, JD, HR, MI, SC, HD)
                                                                                                                                                                                                                                                                                                                                                                                                                                                           PORMAT ('0SAMPLE MEAN: ',F10.4,'
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            PORMAT ('0 SAMPLE MEAN: ',F10.4,'
                                                                                                                                                                                                                                                                                                                                                                                                         FORMAT ('0 SAMPLE MEAN: ', F10.4,'
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         OPROCESSED ', I4,'
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       ,' nI',
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           OPROCESSED ', IU,
                                                                                                                                                                           GENERATE OUTPUT REPORT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           I2, '', A3, ' 19', I2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       OPROCESSED
                                                                                                                                                                                                                                                     WRITE (ICNOUT, 630)
                                                                                                                                                                                                                                                                                                       WRITE (ICNOUT, 640)
                                                                                                                                                                                                                                                                                                                              WRITE (IPRINT, 640)
                                                                                                                                                                                                                                                                              WRITE (IPRINT, 630)
DO 60 J=1,NREPS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      F10.4,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    F10.4.
                                                                                                                                                                                                                                                                                                                                                                                                                                  F10.4)
                                              CONTINUE
                                                                                                                        CONTINUE
                                                                       CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                STOP
                                                                                                                                                                                                                                                                                                                                                                                                                                                           6 10
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             6 20
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             630
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  049
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のなり	SUBROUTINE OPEN (FNAMES) Codssides and sactions as sections as sections and sections are sections and sections and sections are sections are sections are sections are sections are sections and sections are sections are sections are sections are sections and sections are sections are sections and sections are sectio	e e
1 mm		4
C##	OPEN IS A GENERAL PURPOSE SUBROUTINE DESIGNED TO HANDLE ALL	다 #
Cattle	THE OPERATING SUSTEM FILE DEFINITIONS REQUIRED TO INPUT AND	€; 6
S S	OUTPUT DATA TO THE REQUIRED DEVICE. OPEN IS CALLED AS THE	⊕
Catt	PIRST EXECUTABLE STATEMENT OF THE MAIN PROGRAM AND READS A	Ø Ø
C##	DATA PILE TO DETERMINE THE DATA SET REPERENCE NUMBERS (DSRN)	₽
C##	REQUIRED BY THE MAIN PROGRAM. OPEN THEN CALLS THE SYSTEM	ë #
Ctrit	SUBROUTINE PRICHS TO EXECUTE THE CMS PILEDEP COMMANDS WITH	ଣ ଶ୍ର
** O	ARGUMENTS SPECIFIED IN THE DATA PILE. OPEN ALSO INITIALIZES	작 #
C##	A COMMON BLOCK WITH THE DSRN'S ASSIGNED TO MAKE THEM	를 참
C#ID	ACCESSIBLE TO OTHER PROGRAM UNITS.	⇔
COO	TO OPERATE, THE USER MUST HAVE A FILE NAMED 'PNAMES	學
C##	FILES. OPEN READS THE FILE AS POLLOWS:	⇔
\$#C)		ű #
C. \$ \$	LINE 1. FORMAT (415,5X, A8) ASSIGNED TO OUTPUT CONTROL	63 43
CAS	WARIABLE IPRT AND I/O DEVICE NUMBERS FOR	샵 잘
C BC	TERMINAL INPUT, TERMINAL OUTPUT, PRINTER DISK,	公 备
Cata	AND PILENAME FOR PRINT FILE ' <pn> OUTPUT A1'</pn>	€. Ø
C#I	LINE 2. PORMAT (15,5x,7 (A8,2x)) ASSIGNED TO I/O DEVICE	€
Cabo		⇔
C##	PILENAME AND FILETYPE. PILEMODE DEPAULTS TO A1.	ë ₽
CMA	REMAINING VALUES ARE PIVE OR LESS OPTIONAL	합 참
SATA CARD	FILEDEP PARAMETERS, IE. LRECL, BLOCK, ETC.	∰ 6
CBG		산 참
の事件	LINE 2 IS OPTIONAL AND MAY BE LEFT OUT OR REPEATED UP TO	ě Ö
COP	THIRTY TIMES AS NECESSARY.	장 삼
の本語		ě Č
Cases	OTHER SUBROUTINES CALLED: STR\$	₩ ₩
Cto		ە Ø
(4	HRITTEN BY MARK YOUNT AUG 1981	₽
Crist		存
Captri	C 你你们们也也是我们的,我们也是我们的,我们们的,我们们的,我们们的,我们们的,我们们的人们的,我们们的人们的,我们们们的,我们们的人们的,我们们们的,我们们	© #
U		

IMPLICIT REAL® (A-H, 0-Z)

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CALL PRICHS (PAR(1), PRINTS, PAR(3), PNAMES, PAR(4), PAR(5), PAR(6),
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            READ (99, 110, END=30) IDSK (I), DNAMES, DTYPES, (OPTS (J), J=1, 5)
                                                 OUTPUT.
                                                                                               PILES
                                                                                                                                                                                                                                                                                                                          READ DATA FOR TERMINAL I/O AND PRINTER DESTINED OUTPUT
                                                                                                                                                                                                                                                   CALL FRICHS (PAR(1), DNUMS, PAR (3), FNAMES, PAR (12), PAR (5),
                                                                     · PA
COMMON /FILES/ IPRT, ICONIN, ICNOUT, IPRINT, IDSK (30)
                                                                                                                                                                                                                                                                                                                                                                                                                                                      CALL FRICMS (PAR(1), CONINS, PAR(2), PAR(6), PAR(11))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     CALL FRICMS (PAR(1), CNOUTS, PAR(2), PAR(6), PAR(11))
                                                                                                                                                                                                                                                                                                                                                                             READ (99, 100) ITMP, ICONIN, ICNOUT, IPRINT, PNAMES
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               (OPT$(J) .NE. PAR(14)) GOTO 15
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          PAR (7), PAR (8), PAR (9), PAR (10), PAR (11))
                                                                      RECPH
                                               DISK
                                                                                               PERM
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    READ DATA FOR DISK PILE OPERATIONS
                                               TERMINAL .
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        IF (IPRINT .EQ. 6) GOTO 10
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   OPT $ (J) = PAR (13)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    FORHAT (15,5x,7 (A8,2x))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                CNOUT$ = STR$ (ICNOUT)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                PRINTS = STR$ (IPRINT)
                                                                                                                                                                                                                                                                                                                                                                                                                              CONINS = STR$ (ICONIN)
                                                                                                                                                                                                                                                                            PAR (6) , PAR (11)
                                                                                                                                                                                                                                                                                                                                                                                                    FORMAT (415, 5X, A8)
                                                                                                                                                 DIMENSION OPT$ (5)
                                                                                                                                                                                                                            DNUM$ = STR$ (99)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     DO 15 J=1,5
                     REALS PAR(14)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     DO 20 I=1,30
                                               / PILEDEP
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            IPRT = ITHP
                                                                                                 • BLOCK
                                                                                                                                                                                                   IPRT = 0
                                                                        1 Y 1
                                                                                                                                                                                                                                                                                                                                                                                                       100
                                                                                                                                                                                                                                                                                                        000
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IF (IPRT .GE. 20) WRITE (ICNOUT, 200) PAR(1), DNUMS, PAR(3), DNAMES, DTYPES, PAR(6), PAR(11), (OPTS(J), J=1,5)

FORMAT (* ', 7A10/,10X,5A10)

CALL FRICHS (PAR(1), DNUMS, PAR(3), DNAMES, DTYPES, PAR(6), PAR(11), OPTS(1), OPTS(2), OPTS(3), OPTS(4), OPTS(5))
                                                                                                                                                                                              CALL PRICHS (PAR (1))
                                                  DNUMS = STR$(IDSK(I))
                                                                                                                                                                                              .GE. 10)
GOTO 16
                CONTINUE
                                                                                                                                                                                                                REWIND 99
                                                                                                                                                                                             IF (IPRT
                                                                                                                                                            CONTINUE
                                                                                                                                                                            CONTINUE
                                                                                                                                                                                                                                 RET UR N
E ND
                                                                                                      200
                15
                                                                                                                                                            20
30
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A START STARTS	DOUBLE PRECISION FUNCTION STR\$ (IVAL) Chanchardeachdeachae hachaechaechaechaechaechaechaechaechaech	6
•		4
	STR\$ IS A GENERAL PURPOSE PUNCTION INVOKED BY OPEN DESIGNED *	€
		₫
		& #
	SUITABLE AS ARGUMENTS FOR PRICHS. (PRICHS USES ONLY	를 참
	FROM	살
	HUST	Ø ∰
	HT	# #
		各
	STR\$ CONVERTS INTEGER VALUES IN THE RANGE OF +99,999,999 TO	# #
	EON	€: 5
		合件
£ 0		₩ #
** 3	STR\$ RETURNS A CHARACTER VALUE OF 0 IF CONVERSION UNSUCCESSFUL. &	₽
C		₩
	WRITIEN BY MARK YOUNT SEP 1981	4
		Ø
	C 幸福的,可由自己的自己的事情,也是是有一种事情的,他们的,他们也是有一种,他们也会们的自己的自己的自己的自己的自己的,但是他们们们的自己的自己的,但是他们的	ë.
	REAL® B\$, BINK/' '/	
	COMMON /FILES/ IPRT, ICONIN, ICNOUT, IPRINT, IDSK (30)	
	LOGICAL®1 NUM(8), ONUM(8), MINUS/*-"/	
	TOGICAL®1 DIGIT(10)/'0',''','''','''','''''''''''''''''''	
	INTEGERAL FUNC\$/ STR\$ /	
•	RQUIVALENCE (ONUM (1), BS)	
	IP (IPRT .GE. 20) WRITE (ICNOUT, 201) IVAL	
	PORMAT(' INPUT INTEGER = ', I10) IM = 8	
	11	
	IF ((IVAL .GE. 10 498) .OR. (IVAL .LE141047)) GOTO 6000	
	EXTRACT CHARACTERS ONE AT A TIME PROM IVAL AND STORE AS ALPHANUMERIC CHARACTERS IN ARRAY NUM	

```
.GE. 40) WRITE (ICNOUT, 200) IV AL, ONUH (I)
                                                                                                                                                                                                                                                              .GE. 40) WRITE(ICNOUT, 210)
ASSIGNED NEGATIVE IVALUE TO STR$*)
                                                                                        CCAV SETED NUMERIC ', II, ' TO CHARACTER
                                                                            .GE. 40) WRITE (ICNOUT, 200) N, NUM (IM)
                                                                                                                                                         LEPT JUSTIFY CHARACTERS IN B$ (1)
                                                                                                                                                                                                                                                                                                                   ONUM(I) = DIGIT(1)
                                                                                                                                                                                                                                      SUNIW = (I) WONO
            0) GOTO 20
                                                               NUM (IM) = DIGIT (N+1)
                                                 N = N - ITEMP # 10
                                                                                                                                                                                                           30,40,50
                                                                                                                                                                                              GOTO 50
                                                                                                                                                                                                                                                                                                                                                                                                8) GOTO 60
                                     ITEMP = I TEMP
                                                                                                                                                                                                                                                                                                                               IM = IM -
                                                                                                                                                                                                                                                   IM = IM -
IP (IPRT
                                                                                                                                                                                                                                                                                                                                            IF (IPRT
                                                                                                                                                                                                                                                                           PORH AT (*
                                                                                                                                                                                                                                                                                        GOTO 60
                                                                                                                                                                                                                                                                                                                                                          09 CLOS
                                                                                                                                                                                                                                                                                                                                                                                                                                                   CREATE OUTPUT ARRAY
                                                                                                                                                                                                                                                                                                                                                                                                            ONUM (I) = NUM (J)
                                                                                                     - WI = WI
                        N = ITEMP
                                                                                                                                                                                                           IF (IVAL)
            (ITEMP . EQ.
                                                                                                                                                                                                                                                                                                      CONTINUE
                                                                            IP (IPRT
                                                                                                                                                                                                                         CONTINUE
                                                                                         PORMAT ('
                                                                                                                                                                                               (I .GT. 1)
                                                                                                                                                                                                                                                                                                                                                                                                IP (J .GT.
                                                                                                                                                                                                                                                                                                                                                                                   MI + I = C
                                                                                                                                                                                   DO 60 I=1,8
DO 10 I=1,8
                                                                                                                                                                                                                                                                                                                                                                       CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                         CONTINUE
                                                                                                                   CONTINUE
                                                                                                                               CONTINUE
                                                                                                                                                                                                H
                                                                                         200
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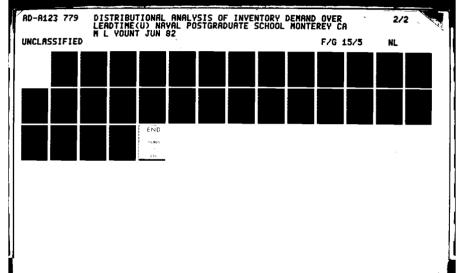
U

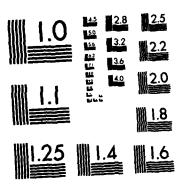
```
IP (IPRT .GE. 30) WRITE (ICNOUT, 220) IVAL, STR$ PORMAT (* NUMERIC VALUE = ', I8, * ALPHANUMERIC VALUE
                                                                                                                                         HRITE (ICNOUT, 6010) FUNC$
FORMAT (* & c & STRING LENGTH BRROR & c & * , A4)
STR = DIGIT (1)
                                                                                      ERROR HANDLING SECTION POLLOWS
STR$ = B$
                                                                                                                             CONTINUE
                                                                                                                                                                                                   RETURN
                                                     RETURN
                                                                                                                                                                                                                        END
                                                                                                                             0009
                                                                                                                                                                6010
                                   220
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유 선 선 선 선 선	4	è	0	은 다	0 6	& ₩	65 69	삼 삼	<u>የ</u> ት	*	€ 5	t T	es T	4 4	찬 참	**************************************	9 0	& ♣	& &	*	INITALOS	4	松油	& *	合併	€ 4	4) 4)	다	6 0			各日	증 참
SUBROUTINE INITAL (PIRST,M.OBS, VBROBS,NBRNEG,应) E. 安泰曼英语安泰安安安安安安安安安安安安安安安安安安安安安安安安安安安安安安安安安	PERST CALLS SUBROUTINE DATARD TO READ ONE SAMPLE	PROM THE SPECIFIED DISK WHEN CALLED FROM THE MAIN	THE STRING OF FOR TY-EIGHT DEMAND OBSERVATIONS THUS READ I	ARE FIRST PROCESSED TO REMOVE ANY NEGATIVE DEMAND	OBSI	IS EQUAL OR LARGER THAN THE NEGATIVE VALUE. WHETHER A		ZERO.			SERIES IS CONSTRUCTED OF ONLY THE NON-ZERO	COUNT STORED, SECOND A THIRD DEMAND SERIES IS		THUS WHEN INITAL RETURN	DEMAND SERIES HAVE BEEN CONSTRUCTED		DEFINITION OF VARIABLES:		COUNT TEMPORARY	N BROBS (2) AND NBROBS (3)	FIRST LOGIC AL VARIABLE TO INDICATE FIRST USE OF		IDSK1	IPRINT 0	IPRT CONTROLS LEVEL OF DIAGNOSTIC	IREV METHOD TO COUNT BACKWARD IN	M I NPUT COUNT OF OB	N BROBS (1) ALWAYS EQUALS !	NBRNEQ COUNTS NUMBER OF SAMPLES W	NBROBS COUNTS OF DBSERVATIONS IN EACH OF ABOVE	NEGOBS LOGICAL VARIABLE, TRUE IF S	OBS (M, 1) ORIGINAL OBSERVATIONS WITH NEGATIV	3 OBS (M, 2) ALL ZERO OBSERVATIONS REMOVED FROM DATA
##U	4	**	13	*	S S S S S S	Catal	C##	をなり	報じ	CO CO CO CO CO CO CO CO CO CO CO CO CO C	会会	€	CAT	C##O	S S S S	を終り	# ()	の存在	C A A	8	C##	CSA	の登録	₽ (%)	なない	の数と	の数数	C	の数数	の存む	CERT	Ç. U	₽ 20

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참
                                         各
                                                                                     如果是多种的人,我们们的,我们也是是一个人,我们们的,我们们的人,我们也是有一个人,我们也会有一个人,我们们的人们的,我们们的人们的人的人,我们们的人们的人们的
                                                         -- DOES ACTUAL READING OF DATA PROM RAW DATA SETS
                                                                                                                                 NBROBS (3)
                                                                                                                                                                                                                                                                                                                                                                                                                                             EDIT BY BACKING OUT AND REMOVING NEGATIVE OBSERVATIONS
                                                                                                                 IPR INT,
                                                                                                                                                                                                                                                   IPR INT,
-- NATURAL LOG OF NON-ZERO OBSERVATIONS
                                                                                                                                                                                                                                                                                                                                                                     WRITE (IPRINT, 600) (OBS (K, 1), K=1, M)
                                                                                                                                                                                                                                                                                                                                          ECHO PRINT INPUT VALUES (CONTROLLED BY IPRT VALUE)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    -OBS (I,1)) GOTO 10
                                                                                                                  ICNOUT,
                                                                                                                                                                                                                                                   ICNOUT,
                                                                                                                                IDSK1,
                           OTHER SUBROUTINES REQUIRED BY INITAL:
                                                                                                                                                                                                                                                                                                                                                                                                                IF (0BS(I,1) .GE. 0.0) GOTO 20
                                                                                                                                                                                                                                                                                                            CALL DATARD (OBS (1,1), M, FIRST, 840)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    IF (OBS(IREV, 1) .LT.
                                                                                                                  ICONIN,
                                                                                                                                                                                                                                                   ICONIN,
                                                                                                                                                             NBRNEG
                                                                                                                                 IREV,
                                                                                                                                                                                                                        FIRST
                                                                                                                                                                                                                                                                                                                                                                                                                                                                           NEGOBS = .TRUE
                                                                                                                                                                                                                                                                                                                                                                     IF (IPRT .GE. 5)
NEGOBS = .FALSE.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       DO 10 J = 2,I
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       IREV = I
                                                                                                                                                                                                                                                                                 IDSK1 = IDSK(1)
                                                                                                                                                                                                                                      COMMON /PILES/
                                                                                                                                                                                                                                                                                               NBROBS (1) = M
                                                                                                                   IPRT,
IDSK (30),
OBS (M, 3)
                                                                                                                                                                                                                                                                                                                                                                                                   DO 20 I=1, H
                                                                                                                                                                                          OBS (M, 3)
                                                                                                                                                                                                                        NEGOBS,
                                                         DATARD
                                                                                                     INTEGERA
                                                                                                                                                COUNT,
                                                                                                                                                                                                         LOGICAL#1
                                                                                                                                                                                                                                                    IPRT,
                                                                                                                                                                                                                                                                   IDSK
                                                                                                                                                                            REALS
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(CONTROLLED BY IPRT)
                                                                                                                                                                                                                                                                                                                                                                                                                                        (OBS (K, 2), K=1, CO UNT)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       WRITE (IPRINT, 630) (OBS (K, 3), K=1, COUNT)
                                                                                                                                                              WRITE (IPRINT, 610) (OBS (K, 1), K=1, M)
OBS(IREV, 1) = OBS(IREV, 1) + OBS(I, 1)
OBS(I, 1) = 0.0
                                                                                                                                                                                                                                                                                                                                                                                                        PRINT NON-ZERO INPUT VALUES (CONTROLLED BY IPRT)
                                                                                                                                                                                           CREATE ARRAY OF ONLY NON-ZERO OBSERVATIONS AND ARRAY OF LOG OF THESE NON-ZERO OBSERVATIONS
                                                                                                                               PRINT EDITED INPUT VALUES (CONTROLLED BY IPRT)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     FORMAT ('1RAW OBSERVATIONS ',3 (T20,20F5.0,/))
                                                                                                                                                                                                                                                                                                                         = LOG(OBS(I,1))
                                                                                                                                                                                                                                                                                                                                                                                                                                       (IPRT .GE. 5) WRITE (IPRINT, 620)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                       PRINT LOG OF NON-ZERO INPUT VALUES
                                                                                                                                                                                                                                                                          (OBS(I,1) . EQ. 0.0) GOTO 30
COUNT = COUNT + 1
                                                                                                                                                                                                                                                                                                          = OBS(I,1)
                                                                                               NBRNEG = NBRNEG +
                                                                                                                                                                                                                                                                                                          OBS (COUNT, 2)
OBS (COUNT, 3)
                                GOTO 20
                                                                = 0.0
                                                                                                                                                                                                                                                                                                                                                                        = COUNT
                                                                                                                                                                                                                                                                                                                                                         = COUNT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       .GE. 5)
                                                                                                                                                              IF (IPRT .GE. 5)
                                                                                                                                                                                                                                                           I=1,H
                                                                OBS (I, 1)
                                                                                                IF (NEGOBS)
                                                CONTINUE
                                                                                                                                                                                                                                                                                                                                                        NBROBS (2)
NBROBS (3)
                                                                                                                                                                                                                                             COUNT = 0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       IF (IPRT
                                                                               CONTINUE
                                                                                                                                                                                                                                                                                                                                          CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      RETURN
                                                                                                                                                                                                                                                           DO 30
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     9
                                                10
                                                                                20
                                                                                                                                                                                                                                                                                                                                           30
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MICROCOPY RESOLUTION TEST CHART NATIONAL BUREAU OF STANDARDS-1963-A

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SUBROUTINE DATARD (MONTH,NBR,TIME,心)		THE VM MINIDISK	PARALLEL ARRAYS OF DATA, THE PIRST THE SEQUENTIAL DAY	ED. ALL THE	AND THEN GROUPED	ACCUMULATED DEMAND	RETURNED FROM	PROCESSED BY					OF DEMAND, DAY 1 TO DAY 1440	FOR EACH ELEMENT OF INPUT DATA	A CCUMULATES DAILY DEMANDS FOR LATER AGGREGATION			STARTING INDEX OF CURRENT 30 DAY MONTH BLOCK	AY MONTH BLOCK	TED IN 30 DAY BLOCKSOR	EATE	IAL DATE	ONLY ON FIRST CALL		() 经运行员的专项目的自己的 医自己的 医克格勒氏性 医克格曼氏征 医克格勒氏征 医克格勒氏征 医克格特氏征 医克格氏征 医克格特氏征 医克格特氏征 医克格特氏征 医克格特氏征 医克格特氏征 医克格氏征 医克格特氏征 医克格特氏征 医克格特氏征 医克格特氏征 医克格特氏征 医克格特氏征 医克格特氏征 医克格特氏征 医克格氏征 医克格特氏征 医克格特氏征 医克格特氏征 医克格特氏征 医克格特氏征 医克格氏征 医克格氏征 医克格氏征 医克格氏征 医克格氏征 医克格氏征 医克格氏征 医克格特氏征性原性 医皮肤炎 医克格氏征 医克格特氏征 医克格特氏征 医克格氏征 医克格特氏征 医克格特氏征 医克格特氏征 医克格特氏征性 医克格特氏征 医克格特氏征 医克格特氏征 医克格特氏征 医克格特氏征 医克格特氏征 医克格氏征 医克格氏征 医克格氏征性 医氏管检验检检验检检验验检验验检验验检验验检验验检验验检验验验验验验验检验验验验验的 医克格氏征性 医克格氏征性 医克格氏征性 医克格氏征性 医克格氏征性 医克格氏性原生 医克格氏征性原生性原生性原生性原生性原生的 医克格氏征性原生性原生的原生性原生性原生性原生性原生的原生性原生的原生性原生性原生的原生性原生的原生性原生的原生的原生的原生的原生的原生的原生的原生的原生的原生的原生的原生的原生的原		IDS K1,	Z					IPR INT,
50.00000000000000000000000000000000000		FROM	, THE FIRST TH	UANTITY DEHAND	I ARE TOTALED	ENTING THE ACC		BE						R EACH ELEMENT	ILY DEHANDS FO	SS	DEMAND DATA	OF CURRENT 30	P CURRENT 30 D	VALUES AGGRAGA	RVATIONS TO CR	DED ON SEQUENT	LE TRUE ONLY O		经基金债券 医多种性性 医多种性性		LAST,	3,	•	QUANT (46)			ICNOUT,
DATARD (MONTH, NBR, TIME, & spectat sectates and sectates		DOES THE ACTUAL READING OF DATA	ARRAYS OF DATA	E SECOND THE Q	DS FOR EACH DA	BUCKETS REPRES	SAMPLE FOR ONE HONTH. THE DATA	W MONTHLY DEMAND DATA TO	L.		VAR I ABL ES:		SEQUENTIAL DATE	ONE ELEMENT FO	A CCUMULATES DA:	DO LOOP INDICIES	INPUT DSRN FOR DEMAND DATA	STARTING INDEX	ENDING INDEX OF CURRENT 30 DAY MONTH BLOCK	OUTPUT DEMAND VALUES AGGRAGATED IN 30	NUMBER OF OBSERVATIONS TO CREATE	QUANTITY DEMANDED ON SEQUENTIAL DATE	LOGIC AL VARIABLE TRUE		医骨骨 经公司 医多种性 医多种性性 医二种性性		PIR ST,	I,	•	MONTH (NBR),			ICON IN,
SUBROUTINE DATARI		DATARD DOES THE	AS TWO PARALLEL !	OF DEMAND AND THE SECOND THE QUANTITY DEMANDED. ALL THE	INDIVIDUAL DEMANDS FOR EACH DAY ARE TOTALED AND	INTO THIRTY DAY BUCKETS REPRESENTING THE	FOR THIS SAMPLE	DATARD IS THE RAW	SUBROUTINE INITAL		DEFINITION OF VAN		DATE 5	J	DEM 1	I, I	IDSK1 1	FIRST	LAST 1	HINOW	1		1		A 你你你你你你你你你你你你你你你你你你你你你你你你你你你你你你你你你你你你	Integerat	IDSK,	DATE (46),	REAL#4	DEH(1550),	LOGICAL#1	COMMON /PILES/	, IPRT,
Captible	Cata	の数数	C#	\$ \$ \$	\$\$	## ()	\$ \$	## ()	の事が	C 454	C#13	\$	C#P	## C## C##	の発売	## C	*	C #	Ç Ç	## **	CO	Cata	Cas	ない では で	CRACTO		•	₹ }		41 7	•	ia*	

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QUANT (I)
                                                                                                                                                                                                                                                                                                                                                                            AGGREGATE ACCUMULATED DEMANDS INTO MONTHLY BUCKETS
                                                                                                                                                                               READ IN DEMANDS AND ACCUMULATE IN DAILY BUCKETS
                                                                                                                                                                                                                                                               .NE. 0)) GOTO 50 = DEM(DATE(I)) +
                                                                                                                                                                                                                                                                                                                      READ (1,810) N, (DATE(I),QUANT(I),I=1,46)
                                                      INITIALIZE COUNTERS USED TO TOTAL DEMAND
                                                                                                                                                                                                           READ(1,810) N, (DATE(I),QUANT(I),I=1,46)
                                                                                                                                                                                                                                                                                                                                                                                                                                                              = MONTH(I) + DEM(J)
                                                                                                                                                                                                                                     IF (.NOT. (N .EQ. 2)) GOTO 70
                          IF (TIME) READ (IDSK1, 800) N
                                                                                                                                                                                                                                                                IF (.NOT. (DATE(I)
                                                                                                                                                                                                                                                                              DEM (DATE (I))
                                                                                                                                                                                                                                                                                                                                                                                                                                               DO 80 J=FIRST, LAST
                                                                                                                                       0.0 = (I) HINCH
                                                                                              0.0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          PIRST = LAST +
                                                                                                                                                                                                                                                                                           CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                              HONTH (I)
                                                                                                                                                                                                                                                  DO 60 I=1,46
              IDSK1 = IDSK(1)
                                                                                DO 20 I=1,1550
                                                                                                H
                                                                                                                                                                                                                                                                                                                                                                                                                                   DO 90 I=1,NBR
                                                                                                                        DO 30 I=1,NBR
                                                                                                                                                                                                                                                                                                          CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                            CONTINUE
                                                                                               DEM (I)
IDSK (30)
                                                                                                                                                                                                                                                                                                                                                                                                        FIRST = 31
                                                                                                                                                                                                                                                                                                                                                                                                                     LAST = 60
                                                                                                                                                                                                                        CONTINUE
                                                                                                            CONTINUE
                                                                                                                                                    CONTINUE
                                                                                                                                                                                                                                                                                                                                                  CONTINUE
                                                                                                                                                                                                                                                                                                                                    GOTO 40
                                                                                                                                                    30
C
                                                                                                                                                                                                                                                                                                                                                  02
C
                                                                                                            20
                                                                                                                                                                                                                                                                                            50
60
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0 NORMAL RETURN 1 INSUPPICIENT DATA (IE. 0 OR 1) 3 STDV EQUALS 0 NUMB ER OF DATA ELEMENTS IN THE SAMPLE SAMPLE STANDARD DEVIATION OF DATA VECT DOUBLE PRECISION SUM OF OBSERVATIONS INPUT DATA VECTOR OF LENGTH N	O H H H H N N N N N N N N N N N N N N N
IEAN OF DATA VECTOR A	

```
GOTO 40

10 CONTINUE
C COMPUTE MEAN AND MOMENT ESTIMATES
C FIND THE MEAN
C SUM = 0.D0
DO 20 I=1,N
SUM = SUM + X(I)
20 CONTINUE
XMEAN = SNGL(SUM)/AN
SUM = 0.D0
DO 30 I=1,N
```

DEV = X(I) - X MEAN $SUM = SUM + DEV \stackrel{\wedge}{=} DEV$

CONTINUE

INE XINV (P. HU, STDV, FX, H Lagarage are are are are are are	SUBROUTINE XINV (P. MU. STDV. FX, MODEL, NPTILE, X, IER) Cerces នេះ ឧទ្ធម្មនិទ្ធមន្ទមនេះ នេះ និះ និះ និះ និះ និះ និះ និង	중 중 중 중 *
I I S	INV IS CALLED BY THE MAIN PROGRAM TO COMPUTE THE ABSCISSA	ě
	FIVE	ů H
-	PERCENTILES OF INTEREST, CURRENTLY THE 75TH, 80TH, 85TH,	公
	90TH AND 95TH PERCENTILES. FOR THE FAMILY OF NORMAL	4
144	DISTRIBUTIONS, (NORMAL, LOGNORMAL AND BERNOULLI-LOGNORMAL)	*
-	CALLS THE IMSL SINGLE PRECISION SUBROUTINE MDNRIS TO	合
-	THE NORMALIZED ABSCISSA VALUE AND THEN CONVERTS THAT	*
_	BY A	다. 경 ·
SAMPLE	MEAN AND STANDARD DEVIATION CONVERSIONS. FOR THE	⊕
~	HIAL, BERNOULLI-EXPONENTIAL AND BERNOULLI-LOGISTIC	ě e
Ш	TIONS, XINV	ě Č
2	SUPPLIED. THE REMAINING	#
NEGATIVE	IE BINOMIAL, LOGISTIC AND LA PLACE, XINV CALLS THE	⇔
5	S POISSN, NEGBIN, LOGIST	*
品	TO COMPUTE THE ABSCISSA VALUES.	春
H	URN TO THE MAIN PRO	*
INVERSE	FOR EACH SAMPLE	Ø Ø
		₩ #
T	ULATIVE PROBABILITY FUNCTION	₽
H	POLLOWING DISTRIBUTIONS SELECTED BY THE VALUE OF THE PARAMETER	샾
HODEL:		e H
		&> ₩
	POISSON	合合
2.	NEGATIVE BINOMIAL	备
	STANDARD NORMAL	哲
	EX PONENTIAL	*
	LOGNORMAL	松谷
	LOGISTIC	삼
	LAPLACE	ě #
	Bernoulli - exponential	*
	BERNOULLI-LOGNORMAL	e Ø
	BERNOULLI-LOGISTIC	샵
		e e

PROBABILITY VALUE COMPLEMENTARY PROBAB ERROR PARAMETER INDI O NORMAL RETURN NE O RETURN CODE FROI OTHER CODE RETURNED OTHER CODE RETURNED C SELECTS DISTRIBUTION E DETERMINES WHICH MU E DETERMINES WHICH MU C SAMPLE MEAN OF EACH C ARRAY OF PERCENTILES BERNOULLI PROBABILIT	E OBABILITY VALUE INDICATING FROM SUBROUTINE NED PROM ROUTINE "MDNRIS" TION MU & STDV EACH MODEL USES ACH GROUP OF DATA ILES FOR TESTING ILITY PARAMETER DEVIATION OF EACH GROUP OF DATA
PROBABILITY VALUE COMPLEMENTARY PROBAB: ERROR PARAMETER INDI O NORMAL RETURN NE O RETURN CODE FROI OTHER CODE RETURNED SELECTS DISTRIBUTION DETERMINES WHICH MU SAMPLE MEAN OF BACH ARRAY OF PERCENTILES ARRAY OF PERCENTILES CONSTANT PI	WALUE BROUTINE BROUTINE "MDNRIS" DV EACH MODEL USES P OF DATA TESTING RANETER N OF EACH GROUP OF INVERSE PUNCTION
COMPLEMENTARY PROBAB ERROR PARAMETER INDIO 0 NORMAL RETURN NE 0 RETURN CODE FROI 0 THER CODE RETURNED SELECTS DISTRIBUTION DETERMINES WHICH MU SAMPLE MEAN OF EACH ARRAY OF PERCENTILES BERNOULLI PROBABILIT	Y VALUE NG BROUTINE "M DNRIS" DV EACH MODEL USES P OF DATA TESTING RANETER N OF EACH GROUP OF INVERSE PUNCTION
ERROR PARAMETER INDIO O NORMAL RETURN NEO RETURN CODE FRO OTHER CODE RETURNED SELECTS DISTRIBUTION DETERMINES WHICH MU ARRAY OF PERCENTILES BERNOULLI PROBABILIT	BROUTINE BROUTINE "MDNRIS" DV EACH MODEL USES P OF DATA TESTING RANETER N OF EACH GROUP OF INVERSE PUNCTION
O NORBAL RETURN NE O RETURN CODE FROI OTHER CODE RETURNED SELECTS DISTRIBUTION DETERMINES WHICH MU SAMPLE MEAN OF EACH ARRAY OF PERCENTILES BERNOULLI PROBABILIT	BROUTINE "BDNRIS" DV EACH MODEL USES P OF DATA TESTING RANETER N OF EACH GROUP OF INVERSE PUNCTION
NEORETURN CODE FROOTHER CODE RETURNED SELECTS DISTRIBUTION DETERMINES WHICH MU SAMPLE MEAN OF EACH E ARRAY OF PERCENTILES BERNOULLI PROBABILIT	BROUTINE "MDNRIS" BOUTINE "MDNRIS" DV EACH MODEL USES P OF DATA TESTING RANETER N OF EACH GROUP OF INVERSE PUNCTION
SELECTS DISTRIBUTION DETERMINES WHICH MU SAMPLE MEAN OF BACH ARRAY OF PERCENTILES BERNOULLI PROBABILIT	ROUTINE "BDNRIS" DV EACH MODEL USES P OF DATA TESTING RANETER N OF EACH GROUP OF INVERSE PUNCTION
SELECTS DISTRIBUTION DETERMINES WHICH MU S SAMPLE MEAN OF BACH ARRAY OF PERCENTILES BERNOULLI PROBABILIT	V EACH MODEL USES OF DATA TESTING AMETER OF EACH GROUP OF
DETERMINES WHICH MU : SAMPLE MEAN OF BACH (ARRAY OF PERCENTILES BERNOULLI PROBABILIT CONSTANT PI	V EACH MODEL USES OF DATA TESTING AMETER OF EACH GROUP OF
SAMPLE MEAN OF BACH ARRAY OF PERCENTILES BERNOULLI PROBABILIT CONSTANT PI	OF DATA TESTING AMETER OF EACH GROUP OF
LE ARRAY OF PERCENTILES BERNOULLI PROBABILIT CONSTANT PI	TESTING AMETER OF EACH GROUP OF
BERNOULLI PROBABILIT	AMETER OF EACH GROUP OF
CONSTANT PI	OF EACH GROUP OF
	OF EACH GROUP OF
STDV SARPLE STANDARD DEVIA	OF TRVERSE PUNCTION
X ABSCISSA VALUE RESULT	
ED RESULT OF	INVERSE PUNCTIONS
OTHER SUBROUTINES REQUIRED BY XINV:	
LAPLCE DISTRIBUTION, DENSITY OR	
MDNRIS INST INVERSE NORMAL SUBRO	ROUTINE
NEGBIN DISTRIBUTION, DENSITY OR	R INVERSE NEGATIVE
BINOMIAL VALUES	
POISSN DISTRIBUTION, DENSITY OR	R INVERSE POISSON VALUES
REAN AND STANDARD DEVIATION ARE	ESTIMATED BY THE METHOD OF
ENTS. FOR DISTRIBUTIONS SUCH AS	THE LAPLACE AND LOGISTIC,
SE ESTIMATORS A	THE CHOICE I
E TO EASE OF COMP	FON.

FX (NPTILE),

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MIYPE (10) /1,1,1,1,3,1,1,2,3,2/,
                                                                                                                                                      HХ
                                                                                                                                                     RETURN X = 0.0 POR COMPOUND DISTRIBUTIONS IF P <=
                                                                                                                                                                                                                                                                                                                                   CALL POISSN(X(J,K), MU(MTYPE(J)), 3, FX(K), IER) IF (IER.NE. 0) GOTO 130
PI/3.1415926/, STDV(3),
                                                                                                                                                                                    X(J,K) = 0.0
IF ((J.GE.8) .AND. (P.LE. HX)) GOTO 110
                                                                                                                                                                                                                                                       GOTO (10, 20, 30, 40, 50, 60, 70, 80, 90, 100), J CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                              INVERSE NEGATIVE BINOMIAL FUNCTION
                                                                                                                                                                                                                                                                                                                                                                                                                                          CALL NEGBIN(X(J,K), MU(MIYPE(J)), STDV(MIYPE(J)), 3, PX(K), IER) IF (IER .NE. 0) GOTO 130
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   INVERSE STANDARD NORMAL FUNCTION
                                                                                                                                                                                                                                                                                                        INVERSE POISSON FUNCTION
                                                                                                                                                                                                                               SELECT THE DISTRIBUTION
                                                NPTILE,
                                                                                                                          HX = 1.0 - FX(K)
     HX,
                                                                                                          DO 120 K=1, NPTILE
                                                                                                                                                                                   0.0 =
                   X (HODEL, NPTILE),
                                                MODEL,
                                                                                                                                                                                                                                                                                                                                                                                 CONTINUE
                                                                                             DO 130 J=1, MODEL
                                                                                                                                                                                                                                                                                                                                                                  GOTO 110
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       GOTO 110
                                  I NT EG ER#4
                                                 IEB,
                                                                              IER = 0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      30
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C
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C
C
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C
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CALL LOGIST(X(J,K), MU(MTYPE(J)), STDV(MTYPE(J)),
3, PX(K), IER)
IF (IER.NE.0) GOTO 140
                                                                                                                                                                                                                                                                                                                                                                                                           CALL LAPLCE(X(J,K), MU(MTYPE(J)), STDV(MTYPE(J)), 3, PX(K), IER)
                                                                                                                                                                                                                     2
                                                                                                                                                                                                                     £
                             1
                                                                                                                                                                                                                    + STDV (MTYPE (J))
                         X (J, K) = HU (HIYPE (J)) + SIDV (HIYPE (J))
                                                                                                           = -MU(MTYPE(J)) * LOG(HX)
                                                                                INVERSE EXPONENTIAL FUNCTION
                                                                                                                                                               INVERSE LOG NORMAL PUNCTION
                                                                                                                                                                                         CALL MDNRIS(FX(K), Z, IER)
IF (IER .NE. 0) GOTO 140
X(J, K) = EXP(MU(MTYPE(J))
                                                                                                                                                                                                                                                                        INVERSE LOGISTIC FUNCTION
CALL MDNRIS(PX(K),Z,IER)
IF (IER .NE. 0) GOTO 130
                                                                                                                                                                                                                                                                                                                                                                                  INVERSE LAPLACE FUNCTION
                                                                                                                                                                                                                                                                                                                                                                                                                                      IF (IER .NE. 0) GOTO 140
                                                                                                           x (J, K)
GOTO 110
                                                     CONTINUE
                                                                                                                                   CONTINUE
                                       GOTO 110
                                                                                                                                                                                                                                GOTO 110
                                                                                                                                                                                                                                              CONTINUE
                                                                                                                                                                                                                                                                                                                                                        CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                  GOTO 110
                                                                                                                                                                                                                                                                                                                                                                                                                                                                CONTINUE
                                                                                                                                                                                                                                                                                                                                           GOTO 110
                                                                                                                                    2000
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                                                      9000
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1.0)
                                                                                                                                                (2
                                                                                                                                              + STDV (MTYPE (J)) #
INVERSE MIXED BERNOULLI-EXPONENTIAL PUNCTION
                                                                                                                                                                                                                                                   = HU(HIYPE(J)) + PACT * LOG(2.0 * P
                                                                             INVERSE BERNOULLI-LOGNORMAL FUNCTION
                                                                                                                                                                                               INVERSE BERNOULLI-LOGISTIC FUNCTION
                          MU(MIYPE(J)) & LOG(P / HX)
                                                                                                                                                                                                                        SQRT(3.0) ¢ STDV(MTYPE(J)
$ (1.0 + TANH(MU(MTYPE(J))
                                                                                                                                IF (IER .NE. 0) GOTO 140 X(J, K) = EXP(HU(HTYPE(J))
                                                                                                                  CALL MONRIS(PR, Z, IER)
                                                                                                                                                                                                                         PACT = SQRT(3.0)
                            18
                                                                                                                                                                                                                                     Z = HX
                        x (J, K)
GOTO 110
                                                                                                                                                                                                                                                 X (J, K)
CONTINUE
                                                  CONTINUE
                                                                                                                                                         GOTO 110
                                                                                                                                                                      CONTINUE
                                                                                                                                                                                                                                                                            CONTINUE
                                                                                                                                                                                                                                                                                        CONTINUE
                                                                                                                                                                                                                                                                                                     CONTINUE
                                                                                                                                                                                                                                                                                                                 RETURN
                                                                                                                                                                    100
                                                                                                                                                                                                                                                              120
                                                 6000
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,FX,IBR) 1844年代本本本本本本本 48.484年代的中央中央中央中央中央中央中央中央中央中央中央中央中央中央中央中央中央中央中央	MONEY WORLD WORKER WORKER	PURPOSE POISSON DISTRIBUTION FUNCTION THE DENSITY OR COMULATIVE DISTRIBUTION	CISSA VALUE OR ALTERNATIVELY, RETURNS THE	PROBABILITY.	SITY AND DISTRIBUTION FUNCTIONS BY USE OF	SS.	40	REPRESENTING ABCISSA VALUES OF THE	DISTRIBUTION. FOR ITYPE = 3, X IS AN OUTPUT ##		***	DESIRED POISSON DISTRIBUTION.	\$Q	GIVEN X	CDF IN FX GIVEN X	INVERSE CDF VALUES IN X GIVEN PX AS CDF		PARAMETER OF PROBABILITY (X<=X). FOR ITYPE = 3, 36		40-40-40-40-40-40-40-40-40-40-40-40-40-4	ERROR PARAMETER RETURN CODE EQUAL TO:		INVALID SELECTION OF TYPE	CONVERGE WITHIN 1000 ITERATIONS.		1. 经表现的现在分词 医克尔特氏 医克克特氏 医克克特氏 医克克特氏 医克克特氏 医克克特氏 医克克特氏 医克克特氏 医克格特氏 医克格特氏 医克格特氏 医克格特氏 医克格特氏 医克格特氏病 计算用的 计记录器 计记录器 计记录器 计记录器 计记录器 计记录器 计记录器 计记录器		IER, TYPE	PDP. FX.	ZL/1.0E-20/	PDF = EXP(-MU)
SUBBOUTINE POISSN (X,MU,TYPE) C各位於中華中国中華中華中華中國中華中國中華中國中華中華中華		CAR FOLSON IS A GENERAL CAR THAT RETURNS EITH FR	VALUE GIVEN THE A	ABSCISSA VALUE GI	COMPUTES POISSON	RECURSION EQUATIO		COC X - INPUT PARAMETER	POISSON	PARAMET		TO - MEAN OF THE	参 母:	TYPE = 1 RETU	2 RETU	3 RETU	Sec.	FX- OUTPUT	PX IS AN I	C等等	IER -	0		-3 -	C P B	1.安徽公司 医安克氏病 医安格氏病 医克格特氏病 经收益的 电电子电子 医电子电子 医电子虫	TNT	SEALS	CDF.	N.	PDF = 0.0 IF (MU .LT. 170.0)

```
(CDF . LT. FX) GOTO 40
                                                                (A .LT. X) GOTO 40
FX = PDF
GOTO 99
                                                                                                      (A .LT. X) GOTO 40
FX = CDF
GOTO 99
                           GOTO 60
GOTO 60
                                            GOTO (10,20,30), TYPE CONTINUE
                                                                                                                                                                                                     PDF
                                                                                                                                                               GOTO 99
                                                                                                                                                                                           IF (PDF .GT. ZL)
                                                                                                                                                                                                    IF (PDF LE. ZL)
CDF = CDF + PDF
                                    IF (TYPE .GT.
                          IF (TYPE .LT.
                 DO 50 I=1,1000
                                                                 IF
                                                                                            CONTINUE
                                                                                                                                   CONTINUE
                                                                                                                                                                         CONTINUE
                                                                                                                                            ΗF
CDF = PDF
                                                                                                                                                                                                                       CONTINUE
                                                                                                                                                                                                                                 IER = -3
                                                                                                                                                                                                                                                    CONTINUE
                                                                                                                                                                                                                                                             IER = -1
                                                                                                                                                                                                                                                                       CONTINUE
        A = 0.0
                                                                                                                                                                                                                                          GOTO 99
                                                                                                                                                                                                                                                                                RETURN
                                                                                                                                                                                                                                                                                         E ND
                                                                                             20
                                                                                                                                   30
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	3 I, TER, TYPE	
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*	· Carlotte and the second and the se	の数の
ö	d -3 - ALGORITHM DID NOT CONVERGE WITHIN 1000 ITERATIONS.	Cec
ĕ	-	Cress
*	O - NORMAL RETURN	の意味
Ö	* IER - ERROR PARAMETER RETURN CODE EQUAL TO:	の特殊
ü		なない
Ö	C PX IS AN INPUT PARAMETER.	C Str
ă.	the fix-output parameter of probability (x<=x). For type = 3,	CES
ö		の登録
ö	& RETURNS INVERSE CDF VALUES IN X GIVEN PX AS CDF	S S S S S
ŏ	2 RETURNS	C S
ø	\$ TYPE = 1 RETURNS PDF IN FX GIVEN X	Carried Carrie
Ö		C SE
¥	DISTRIBUTION.	
ě	& STDV - STANDARD DEVIATION OF THE NEGATIVE BINOMIAL	C##
ä		Ces
ö	* MU - MEAN OF THE NEGATIVE BINOMIAL DISTRIBUTION.	C C
ä		Ctgt
益	AN OUTPUT PARAMETER.	Ceta
ā	NEGETIVE BINOMIAL DISTRIBUTION. FOR 1	から
Ö	4 X - INPUT PARAMETER REPRESENTING ABSCISSA VALUES OF THE	な業と
¥		CAR
ö	BY USE OF RECURSI	# * U
*	COMPUTES NEGATIVE BINOMIAL	E U
ä	RETURNS THE	数はい
ě	DISTRIBUTION VALUE GIVEN THE ABSC	の意味
ä	FUNCTION THA	8
#	A NEGBIN IS A GENERAL PURPOSE NEGATIVE BINOMIAL DISTRIBUTION	CAR
ğ	•	S C
なる	20DEOUTER SECONTRA (A) HO() JULY 1 LE	Ë
	TORT OR GOOD HOLD HE AT MIGURE GRANDLOGGING	

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+ K - ONE) 4 (ONE - RHO) 4 PDP /
X,
ZL/1.0E-20/
                                                                                                                                                                                                                        IF (CDF .LT. PX) GOTO 40
                                                                                                                                    IF (A .LT. X) GOTO 40
PX = PDF
GOTO 99
                                                                                                                                                                             IP (A .LT. X) GOTO 40
PX = CDP
GOTO 99
VAR,
ONE /1.0/,
                                                                                          IF (TYPE .LT. 1) GOTO 60
IF (TYPE .GT. 3) GOTO 60
GOTO (10,20,30), TYPE
                                                                                                                                                                                                                                            GOTO 99
                                                                                                                                                                                                             CONTINUE
                                                                                                                            CONTINUE
                                                                                                                                                                    CONTINUE
                                                                                                                                                                                                                                                                A = A + ONE
                                                                                  DO 50 I=1,1000
                    VAR = STDV3F2
                                                                                                                                                                                                                                                      CONTINUE
                                                                                                                                                                                                                                                                            IF (PDF
                                         K = MU442
STDV.
                                                                                                                                                                                                                                                                                                         CONTINUE
                                                                                                                                                                                                                                                                                                                               GOTO 99
                                                   PDF :
                                                              CDF
                                                                                                                                                                    20
                                                                                                                                                                                                             30
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CONTINUE IER = -1 CONTINUE RETURN

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电影像 经保存款 电电流存储器 化电影电影		ION FUNCTION	DISTRIBUTION	Y, RETURNS THE	•		SA VALUE OF				METHOD OF MOMENTS			DISTRIBUTION OR					GIVEN FX AS CDF		FOR TYPE = 3,							非常的现在分词的现在分词的现在分词的				ONE /1.0/.	×	
SUBROUTINE LOGIST (X, MU,STDV,TYPE,FX,IER)		LOGISTIC DISTRIBUTION	THE DENSITY OR CUMULATIVE DISTRIBUTION	VALUE OR ALTERNATIVELY, RETURNS	PROBABILITY.		REPRESENTING THE ABSCISSA	FOR 1			DISTRIBUTION OR ME			OF THE LOGISTIC DI	MLE ESTIMATE.		FX GIVEN X	GIVEN	CDF VALUES IN X G		PROBABILITY (X<=X).			RN CODE EQUAL TO:		OF TYPE		Cases no separate se				HALF/0.5/,	SQRPI,	
L N OLS N (X) H OLS LD N (X) TSID		GENERAL PURPOSE LO					INPUT PARAMETER REPRESI	THE LOGISTIC DISTRIBUTION.	PAR AMETER.		MEAN OF THE LOGISTIC D	OR MLE ESTIMATE.		STDW- STANDARD DEVIATION OF	HOME NTS OR		RETURNS PDF IN F	CDF IN	INVERSE		OUTPUT PARAMETER OF PRO	PX IS AN INPUT PARAMETER.		ERKOR PARAMETER RETURN	NORMAL RETURN	INVALID SELECTION		1. 多年的 医多种性 医多种性 医多种性 医多种性		TYPE		FX,		
SUBROUTINE LOGIST		LOGIST IS A G	THAT RETURNS EITHER	VALUE GIVEN TI	ABSCISSA VALU		X - INPUT		OUTPUT		MU- MEAN O	OR MLE		STDV- STAN	RETHOD OF		TYPE = 1	2			PX- OUTPUT	FX IS		IER - ERKO) · 0	-1 - II		· 李安安安安安安安安安安安安安安	INTEGER	* IBR,	REALCH	a ARG,	PI/3.1415926/	
な芸術をし	300	C# 53	CAS	C##	S	の事件	の数の	ない。	0##C	の権権	の数の	の数数	E S	公会 ひ	100 PM	C#40	C.	CBB	の数数	の事件	C本語	の事件	の数字	の作物	C#C	の数の	Critical	の事がかれ	,					

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COMPUTE X VALUES PROM PROBABILITY INTEGRAL TRANSPORM
                                                                                                                                                                                                                                                                 STDW * SQRT3 & LOG(PX / (ONE - PX)) / PI
                                                                                                                          SECHX = ONE / COSH(ARG)
PX = PI * SECHX**2 / (4.0 * SORT3 * SIDV)
                                     GOTO 40
GOTO 40
TYPE
                                                                                                                                                                                                FX = HALP * (ONE + TANH (ARG))
GOTO 50
CONTINUE
                                                                                                     COMPUTE DISTRIBUTION PDF
                                                                                                                                                                               COMPUTE DISTRIBUTION CDF
         INITIALIZE CONSTANTS
                                                          GOTO (10,20,30), CONTINUE
                              SORT3 = SORT (3.0)
ARG = HALF * PI *
                                                                                                                                                                                                                                                                 X = MU +
                                                                                                                                                                                                                                                                                                 IER = -1
                                                                                                                                                                                                                                                                          GOTO 50
CONTINUE
                                                                                                                                               GOTO 50
                                                  IP (TYPE .LT.
                                                                                                                                                          CONTINUE
                                                                                                                                                                                                                                                                                                           CONTINUE
                                                                                                                                                                                                                                                                                                                     RETURN
                                                                                2000
                                                                                                                                                          2000
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C
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	OR MLE	ESTIMATE.			
	STDV- STANDARD	ARD DEVIATION	OF THE LAPLACE D.	DISTRIBUTION OR	
	METHOD	OF HOMENTS OR	MLE ESTIMATE.	`	
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	TYPE = 1 R	RETURNS PDF IN	FX GIVEN X		
	2 B	RNS	PX GIVEN X		
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= MU + STDV \approx LOG(TWO * PX) / SQR2
= MU - STDV * LOG(TWO - TWO * PX) / SQR2
                                                                                                                                                                                                                                                                         COMPUTE X VALUES PROM PROBABILITY INTEGRAL TRANSFORM
                                                                                                                                                                                                                        IF (x . GE. ZERO) FX = ONE - PX
GOTO 50
                                                                                                                                 PX = EXP(-ARG) / (SQR2  RSTDV)
GOTO 50
                                                                                                                                                                                    COMPUTE DISTRIBUTION CDP
                                                                                                          COMPUTE DISTRIBUTION PDF
                                 = SQR2 * ABS(X - MU) / STDV
(TYPE .LT. 1) GOTO 40
(TYPE .GT. 3) GOTO 40
                                                                                                                                                                                                            PX = EXP(-ARG) / THO
                                                                                                                                                                                                                                                                                               IF (FX . LT. 0.5)
IF (FX . GE. 0.5)
GOTO 50
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          INITIALIZE CONSTANTS
                                                          IF (TYPE .GT. 3)
GOTO (10,20,30),
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SUBROUTINE SAMPLE (ISEED,) DBR, I, MODEL, NPTILE, X, PX, PHAT, MSE)		SAMPLE IS THE HEART	IG BY THE MAIN PROGRAM TO GENERATE SUCCESSIVE REPETITIONS OF	THE PSEUDO SAMPLES FOR THE PURPOSE OF AVERA	4 THE RANDOM INTEGERS PROM ONE TO PORTY-EIGHT ARE OBTAINED	EXPANDING FORTY-EIGHT ZERO TO ONE RANDOM NU	IN MULTIPLYING BY PORTY-EIGHT, ADDING ONE AND TRUNCATING TO		DEMAND OBSERVAT			EARLIER BY XINV AND	OBSERVA	VALUE. SUCCESSES AF		IN THE CASE OF INTEGER ABSCISSA VALUE, FOR THE POISSON AND		DISTRIBUTIONS	WERE RECORDED ONLY UNTIL THE NUMBER OF	THAN THE EXPECTED	PERCENTILE TIMES THE NUMBER OF OBSERVA	APTER THE ENTIRE	а	ACCUMULATOR VARIABLE PHAT FOR LATER OUTPUT. LIKEWI	MEAN SQUARED	A VARIABLE MSE POR LATER OUTPUT	₩	te Variables used are as Pollows:		W A DUMMY ARRAY FOR RANDOM NUMBERS FOR SAMPLERAP	AN	BPROB	EX PS E	d FX PRABABILITIES OF INTEREST
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CONTROL PARAMETER POR OUTPUT OF DIAGNOSTIC INFO
                                                                                          DO INDEX SEQUENCING THROUGH SAMPLERAP SAMPLES
                                                                                                                                                                                    A RRAY OF DEMAND OBSERVATIONS AND DERIVATIVES
                                                                                                        INDEX TO SELECT RANDOM OBSERVATION PROM OBS
                                                                                                                                                                                                                                  NUMBER OF BERNOULLI SUCCESSES EACH TRIAL
                                                                            PERCENTILES
                                                                                                                                                                                                                                                 EXPECTED DEMAND OBSERVATION FOR A GIVEN
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                                             S EED FOR RANDOM NUMBER GENERATOR LRND
                                                                                                                                                                                                                   SEUDO SAMPLE OF DEMAND OBSERVATIONS
                                                           DO INDEX SEQUENCING THROUGH MODELS
                                                                                                                                      MEAN SQUARED ERROR OF PERCENTILES
                                                                                                                                                     NUMBER OF OBSERVATIONS IN SAMPLE
                                                                                                                                                                                                                                                                                                                                                                                                        PHAT (3, MODEL, NPTILE)
                                                                                                                                                                                                  UMULATIVE PERCENTILE ESTINATES
                                                                                                                                                                     UMBER OF PERCENTILES TO TEST
                                                                           DO INDEX SEQUENCING THROUGH
                                                                                                                                                                                                                                                                                                                                                                                                                       X (MODEL, NPTILE),
                                                                                                                       HUNBER OF MODELS TO TEST
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    ICNOUT,
                                                                                                                                                                                                                                                                                                                                                                                                                                     FX (NPTILE),
                                                                                                                                                                                                                                                                                                                            HODEL.
                                                                                                                                                                                                                                                                                                                                                         IPRT,
                             DSRN POR PRINTER DISK
                                                                                                                                                                                                                                                                PERCENTILE AND MODEL
                                                                                                                                                                                                                                                                                                                                                                                                                                                      EXPS (10)
                                                                                                                                                                                                                                                                                                                                                                                        BPROB,
DEMAND CATEGORY
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   ICONIN,
                                                                                                                                                                                                                                                                                                                                                                                                                      MSE (3, MODEL, NP TILE),
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               = PX(K)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  10 K=1,NPTILE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   = PLOAT (NBR)
                                                                                                                                                                                                                                                                                                                                                                                                                                      OBS (NBR, 3),
                                                                                                                                                                                                                                                                                                                                                                                                                                                                     COMMON /PILES/
                                                                                                                                                                                                                                                                                                                                                                                                        SAMP (48),
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  IDSK (30)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 EXPS (K)
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                                                                                                                                                                     NPTILE
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FOR NON-INTEGER VALUES OF EXPECTED DEMAND,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          IN THE CASE OF INTEGER VALUES OF EXPECTED
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            SAMPLE, IS LESS THAN OR EQUAL TO EXPECTED
                                                                                                                                                                                                                                                                                                                                                                                                                                                                         ACTUAL DEMAND, REPRESENTED BY THE PSEUDO
                                                                                                                                                                                                                                                                                                                                                                                                                                                      ACCUMULATE BERNOULLI SUCCESSES WHENEVER
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              DEMAND, SUCCESSES ARE ACCUMULATED UNTIL
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  THE EXPECTED NUMBER OF SUCCESSES IS
                                                                                                                                                                                                                                                                                                                                                                      IF (.NOT. (SAMP(L) .LE. X(J,K))) GOTO 60
IF (AMOD(X(J,K),1.0) .EQ. 0.0) GOTO 30
                                                                                                                                                                                     WRITE (IPRINT, 600) (SAMP(L), L=1, NBR)
                                                                                                                                                                                                                             COMPUTE SAMPLE PERCENTILES FOR BACH PSEUDO SAMPLE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            SUCCES = SUCCES
                                                                                                                                                                                                                                                                                       (IPRT .GE. 5) WRITE (IPRINT, 610)
80 K=1, NPTILE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        REACHED.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    DEMAND.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   CONTINUE
                                                                                                                        IND = IPIX(A (L) * AN)
                                                                                CALL LRND (ISEED, A, NBR, 2,0)
                                                                                                                                           SAMP (L) = OBS (IND, 1)
                                      GENERATE PSEUDO SAMPLES
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                GOTO
                                                                                                                                                                                                                                                                                                                                                   DO 70 L=1, NBR
                                                                                                                                                                                                                                                                                                                            SUCCES = 0
                                                                                                                                                                                     IF (IPRT .GE. 5)
                                                                                                                                                                                                                                                                  90 J=1, HODEL
                                                                                                  DO 20 L=1,NBR
                                                                                                                                                                CONTINUE
CONTINUE
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IF (PLOAT(SUCCES) .GE. EXPS(K)) GOTO 40 SUCCES = SUCCES + 1

J

CONTINUE	CONTINUE	CONTINUE	CONTINUE	BPROB = FLOAT (SUCCES) / AN	IF (IPRT .GE. 5) WRITE (IPRINT, 620) X (J, K), BFROB, FX (K)		ACCUMULATE SQUARED ERROR AND ESTIMATED PERCENTILE	POR EACH DISTRIBUTION AT EACH THEORETICAL PERCENTILE		PHAT(I,J,K) = PHAT(I,J,K) + BPROB	MSE(I,J,K) = MSE(I,J,K) + (BPROB - PX(K))	IP(IPRT . GE. 5) WRITE (IPRINT, 630) PHAT (I, J, K), MSE (I, J, K)	
0	20	9	70			ပ	ပ	ပ	ပ				

630

6 00 6 10 6 20

CONTINUE

CONTINUE

60 0 64	SUBROUTINE OU	SUBROUTINE OUTPUT (MODEL, NPTILE, NRRPS, FX, IC, PHAT, MSE, CAT)
ないので		
C##	OUTPUT IS THE	FINAL SUBROUTINE CALLED BY THE MAIN PROGRAM
Cato	8	TO GENERATE THE OUTPUT REPORT. ONLY MINOR
C#	COMPUTATIONS ARE	ARE PERFORMED BY OUTPUT, THOSE BEING COMPUTING
	THE AVERAGE P	AVERAGE P VALUE AND ITS STANDARD DEVIATION, AVERAGING
の作品	THE HEAN SQUA	SQUARED ERROR AND TOTALING THE AVERAGE HEAN SQUARED
C SEC	ERROR FOR EAC	EACH DEMAND CLASS AND HODEL.
の数数		
C##	DEPINITION OF	WARIABLES:
の存む		
C SEC	CAT	BREAKPOINTS OF DEMAND CATEGORIES FOR LOW,
C##		HIGH DEMANDS
Cest	DISTR	CHARACTER NAME OF EACH MODEL TESTED
C##	PX	DISTRIBUTION PERCENTILES TO TEST
の発験	H	DEMAND CATEGORY FOR SAMPLE UNDER TEST
C##	IC	COUNT OF SAMPLES IN EACH DEMAND CATEGORY
Cost	IP RI NT	DSRN OF PRINTER DISK
C#	ט	DO INDEX SEQUENCING THROUGH MODELS
C##	¥	DO INDEX SEQUENCING THROUGH PERCENTILES
C##	MODEL	NUMBER OF MODELS TO STUDY
9 8 0	MSE	MEAN SQUARED ERROR OF PREDICTED VS. ACTUAL
の数数		P ERCENTILE S
COO	DW	BERNOULLI MEAN OF PSEUDO SAMPLE REPETITIONS **
の事件		FOR EACH PERCENTILE AND MODEL TESTED
040 040	NPTILE	NUMBER OF SAMPLE PERCENTILES TO TEST
Cest	ທ	NUMBER OF PSEUDO SAMPLE REPETITIONS
Cris	PH AT	CUMULATIVE PERCENTILE ESTIMATES FOR EACH
C # 45		DEMAND CATEGORY, MODEL AND PERCENTILE
₩	STDV	
の登録		REPETITIONS FOR EACH PERCENTILE AND
できな		MODEL TESTED
の権力	THSE	RE ERROR SUMME
Cra		CH DEMAND
の数数	TRIALS	TOTAL NUMBER OF REPETITIONS. USED TO NORMALIZE &

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PINAL FIGURES. COMPUTED AS COUNT OF LINE ITEMS & A PER DEMAND CATEGORY TIMES NREPS
                                             * BERNOULLI-EX PONENTIAL *
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     IF ((J .EQ. 1) .OR. (J .EQ. 4) .OR. (J .EQ. 8))
WRITE(IPRINT, 600) NREPS, IC(I), RANGE(I), CAT(I), CAT(I+1)
                                                                                                                                                                                                                                                                                                                    BERNOULLI-LOGISTIC'/
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       = SQRT(MU(K) + (1.0 - MU(K)) / TRIALS)
                                                                                                                                                                                                                                                  *NEGATIVE BINOMIAL*
                                                                                                                                                                                                                                                                                                                                                     I PR I NT.
                                                                                IC (3),
                                                                                                 IPRINT
                                                                                                                                                 PHAT (3, MODEL, NPTILE),
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       DISTR (J), (PX (K), K=1, NPTILE)
                                                                                                                                                                                                                                                                   EXPONENTIAL',
                                                                                                                                                                                                                                                                                 'LA PLACE',
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        / TRIALS
                                                                                                                                CAT (4),
                                                                                                                                                                 MU (10),
                                                                                                                                                                                                                                                                                                                                                    ICNOUT,
                                                                                                NPTILE,
                                                                                                                                                                                 TRIALS
                                                                                                                                                                                                                                                                                                                     BER NOULLI-LOGNORMAL",
                                                                                                                                                                                                                  RANGE (3) /'LOW', 'MEDIUM', 'HIGH'/
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        MU(K) = PHAT(I,J,K)
                                                                                                                                                                                                                                                                                                                                                                                                                                                      GOTO 30
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      WRITE (IPRINT, 610)
                                                                                                                                                                                                                                                                                                                                                    ICON IN,
                                                                                                                                                                                                                                                                                  · LOG NORMAL .
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       DO 10 K=1,NPTILE
                                                                                                                                                                                                                                                                                                   . LOG ISTIC.
                                                                                                 NREPS,
                                                                                                                                                                                                                                                                                                                                                                                                                                      TRIALS = FLOAT (IC(I)
                                                                                                                                                                                                                                                  DISTR (10) / POI SSON',
                                                                                                                                                                                                                                                                                                                                                                                                                                                     IF (TRIALS .EQ. 0.0)
                                                                                                                                                  MSE (3, MO DEL, NP TILE),
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       IF ((J .EQ. 1)
                                                                                                                                                                                                                                                                   NOR MAL"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        STDV (K)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        TMSE = 0.0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                      DO 20 J=1, MODEL
                                                                                                                                                                                                                                                                                                                                                                                                     CAT(3) = CAT(3)
                                                                                                                                                                                                                                                                                                                                                                                      CAT(2) = CAT(2)
                                                                                                                                                                                                                                                                                                                                     COMMON /FILES/
                                                                                                                                  FX (NPTILE)
                                                                                                                                                                                  STDV (10),
                                                                                                                                                                                                                                                                                                                                                                                                                      DO 30 I=1,3
                                                                                                                                                                                                                                                                                                                                                                     IDSK (30)
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                                                                                                HODEL,
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PORMAT (6X,12, REPETITIONS FOR EACH OF ',14, PSEUDO SAMPLES',/,
                                                                                                                                                                                                                                                                                                  ,5F10.6, /, TOTAL MSE: ', F8.2, 'E-04")
                                                                                                                                                                                                      6X,A7, DEMAND RANGE: ', P5.1, ' < D < ', F7.2, ' PER YEAR')
                                                                                                             WRITE (IPRINT, 640) (MSE (I,J,K),K=1,NPTILE),TMSE
                                                                                                                                                                                                                                           * ESTIMATES , 22x, PERCENTILES (P) ', /, 12x, 5F10.2)
                                                                       (STDV (K), K=1, NPTILE)
/ TRIALS
                                                     (MU (K), K=1, NPTILE)
                 THSE = THSE + HSE(I,J,K)
= MSE (I,J,K)
                                                                                                                                                                                                                      FORMAT (/, DISTRIBUTION: ', 2A16,/,
                                                                                                                                                                                                                                                             ', 5F10.6)
                                                                                         THSE = THSE # 1.0E04
                                                                                                                                                                                                                                                                                , 5F10.6)
                                                    WRITE (IPRINT, 620)
WRITE (IPRINT, 630)
MSE (I, J, K)
                                  CONTINUE
                                                                                                                                                                                                                                                                                 STD DEV
                                                                                                                                                                                                                                                             FORMAT ( MEAN
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